

# Terrestrial Reference Frames

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**EGU and IVS Training School on VLBI for  
Geodesy and Astrometry**

**March 2-5, 2013, Aalto University, Espoo, Finland**



# Outline

- Global terrestrial reference frames
- The Terrestrial and the Celestial Reference Frame
- Regional reference frames
- Applications of reference frames
- References

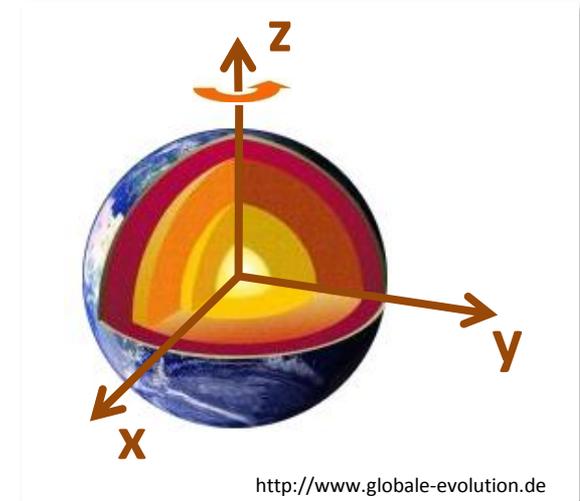
# Global terrestrial reference frames

- The International Terrestrial Reference System (ITRS)
- The ITRS realization DTRF2008 computed by DGFI
- The research topic: epoch reference frame

# International Terrestrial Reference System

## Definition

- Origin: Centre of mass of the Earth
- Unit length: Meter (SI)
- z axis: mean Earth rotation axis
- x and y axis in equatorial plane
- X axis intersects Greenwich meridian



## Realization

- By positions and velocities of global distributed observing stations of the geodetic space techniques
    - Global Navigation Satellite Systems (GNSS (GPS, GLONASS))
    - Very Long Baseline Interferometry (VLBI)
    - Satellite Laser Ranging (SLR)
    - Satellite based Doppler measurement system (DORIS)
- International Terrestrial Reference Frame (ITRF)

# International Terrestrial Reference Frame

... is the basis for

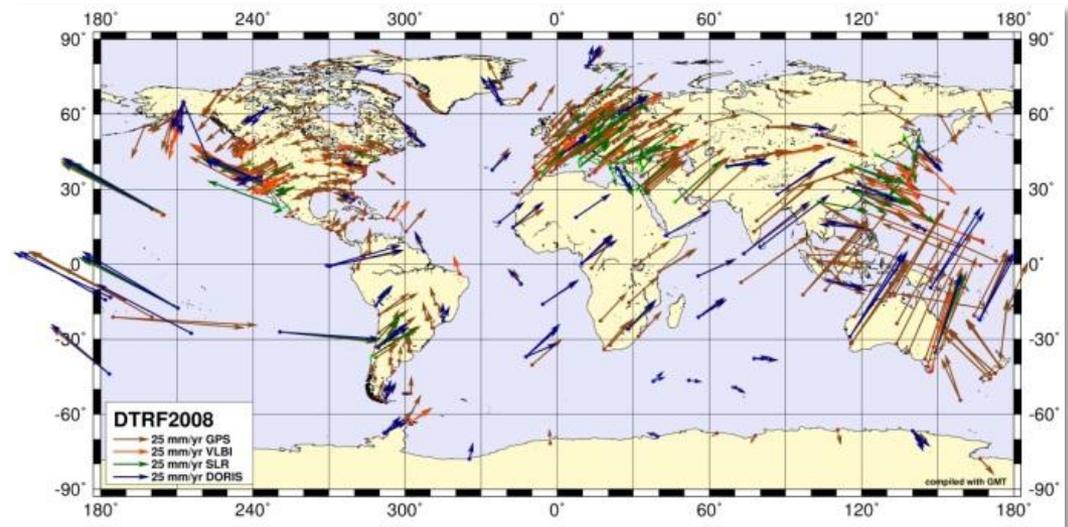
the determination of the Earth's figure and its orientation in space

- Referencing of processes at the Earth and in its near environment (Geo referencing)
  - Geophysical processes (plate tectonics, Earthquakes, ocean dynamics ...)
  - Determination of satellite orbits

- Positioning, Navigation

→ It is a fundamental component of the Global Geodetic Observing System (GGOS)

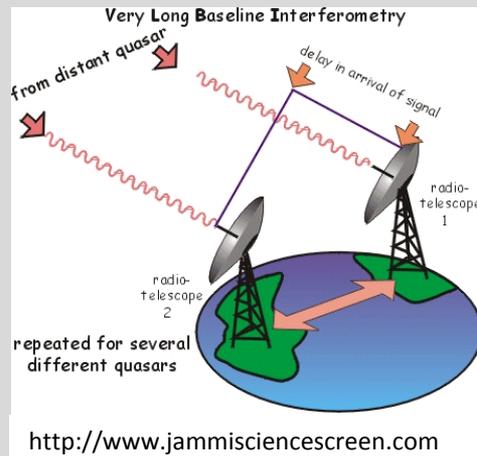
- Examples for applications will be given at the end of the lecture



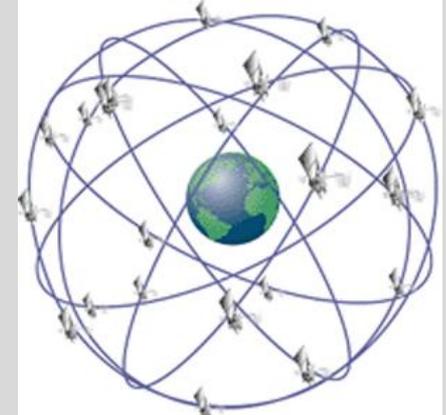
Realization computed at DGFI: DTRF2008

# Geodetic space observation techniques

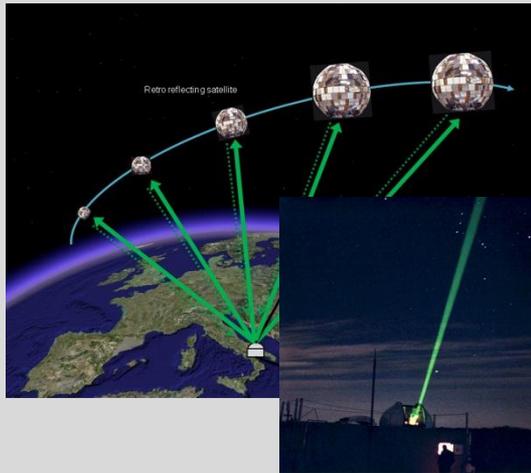
## Very Long Baseline Interferometry (VLBI)



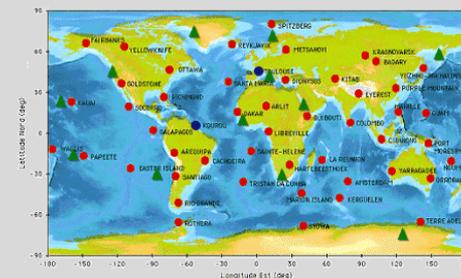
## Global Navigation Satellite Systems (GNSS)



## Satellite Laser Ranging (SLR)



## Doppler Orbitography and Radiopositioning Integrated by Satellite (DORIS)

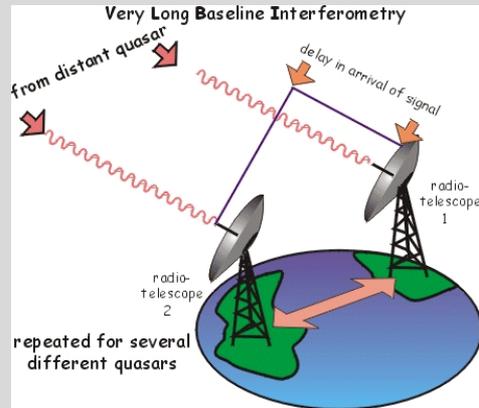


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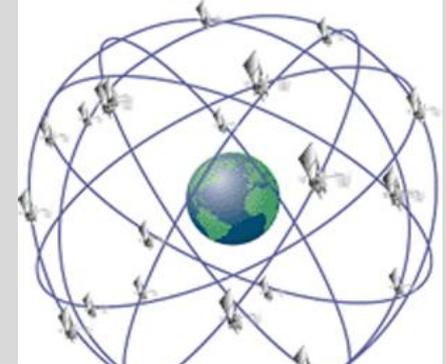


# Geodetic space observation techniques

## Very Long Baseline Interferometry (VLBI)

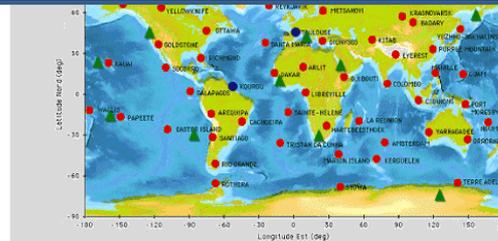
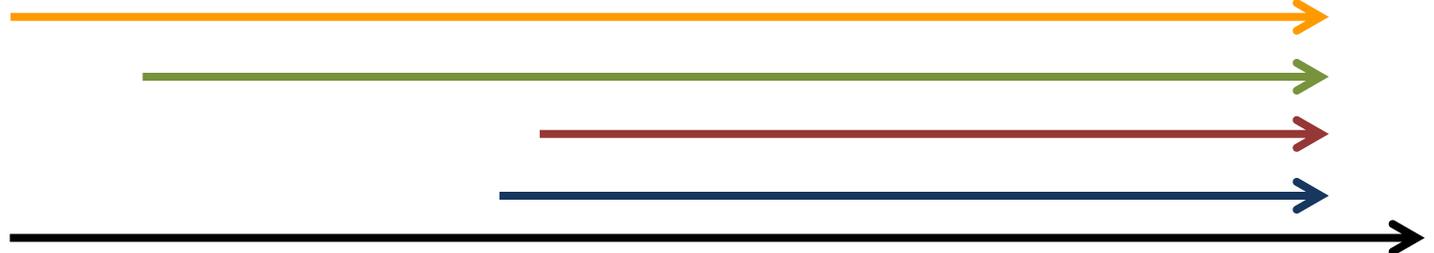


## Global Navigation Satellite Systems (GNSS)



VLBI  
SLR  
GNSS  
DORIS

1980 1985 1990 1995 2000 2005 2010



<http://www.cls.fr>



# Observation techniques: pros,cons

## VLBI:

**pro:** the only observation techniques, which observes extragalactic objects and hence allows for the determination of all **Earth Orientation Parameters (EOP)**. The **scale** is determined with high accuracy.

**con:** few stations with suboptimal global distribution → poor accuracy of temporal highly resolved parameters (e.g. EOP)

## SLR:

**pro:** low orbiting (high sensitivity), spherical satellites (good modeling) allow for the determination of the **center of mass of the Earth** with high accuracy. The **scale** is also determined with high accuracy.

**con:** few stations with suboptimal global distribution → poor accuracy of temporal highly resolved parameters (e.g. EOP)

# Observation techniques: pros,cons

## GNSS:

**pro:** a large number of stations and observations lead to a high precision of the determined parameters.

**con:** forces on the satellites difficult to model → systematic effects in the realized centre of mass

## DORIS:

**pro:** a lot of stations with a good global distribution

**con:** low accuracy of observation (centimetres)

# Combination of the techniques

- **Means?** Determination of geodetic parameters from the observations of all techniques in one adjustment
- **Why?** Strengths of the several techniques can be exploited, weaknesses are balanced; high redundancy
- **How?** At DGFI by addition of normal equation systems (Gauß-Markov-Model) of the different observation techniques

# Realisation of the ITRS – Structure of the relevant IAG-Services

## IAG: International Association of Geodesy

### Technique Services

IGS (GNSS)

IVS (VLBI)

ILRS (SLR)

IDS (DORIS)

### International Earth Rotation and Reference Systems Service

IERS

ITRS  
Combination  
Centre (IGN)

EOP  
Combination  
Centre

ITRS  
Combination  
Centre (DGFI)

ITRS Product  
Centre

ICRS Product  
Centre

Computation  
of the IERS  
products

Selection of one of  
the solutions  
and provision

# Input data for DTRF2008

## Processing within Technique Services

- An international service is responsible for the analysis of the observations of each observing technique and the generation of the products
- Observations are processed by the Analysis Centres of the service ...
- The results are combined by the Combination Centre (weekly or session-wise) (Result: one data set per technique)
- The processing is done using common standards (DTRF2008: Conventions IERS2003; current: IERS2010, plus technique-specific models)

*Input data for ITRF2008 and DTRF2008*

Technique	Service	Time span	Resolution	Typ
GNSS	IGS	1997-2008	weekly	solution
VLBI	IVS	1980-2008	session	NEQ
SLR	ILRS	1983-2008	fortnightly, weekly	solution
DORIS	IDS	1993-2008	weekly	solution

# Geodetic parameters...

... derived from the observations of the four observation techniques and relevant for the ITRF

	Station coordinates	Earth Orientation Parameters (EOP)				Indirect parameters: datum parameters	
		Terrestrial pole	$\Delta$ UT1	Length of day (LOD)	Nutation parameters	Origin	Scale
<b>VLBI</b>	X	X	X	X	X		X
<b>SLR</b>	X	X		X		X	X
<b>GNSS</b>	X	X		X			
<b>DORIS</b>	X	X		X			

Technique-specific parameters are consistently estimated but reduced, e.g. orbit and clock parameters, atmospheric parameters, ambiguities, range biases, ... .

# Geodetic parameters...

... derived from the observations of the four observation techniques and relevant for the ITRF

	Station coordinates	Earth Orientation Parameters (EOP)				Indirect parameters: datum parameters	
		Terrestrial pole	$\Delta$ UT1	Length of day (LOD)	Nutation parameters	Origin	Scale
<b>VLBI</b>	X	X	X	X	X		X
<b>SLR</b>	X	X		X		X	X
<b>GNSS</b>	X	X		X			
<b>DORIS</b>	X	X		X			

Only VLBI can determine  $\Delta$ UT1 and Nutation parameters in an absolute sense! → VLBI is the only technique which contributes to the realizations of ITRS and the Int. Celestial Reference System ICRS (Session 3.5) and provide the transformation parameters between ITRF and ICRF.

# Geodetic parameters...

... derived from the observations of the four observation techniques and relevant for the ITRF

	Station coordinates	Earth Orientation Parameters (EOP)				Indirect parameters: datum parameters	
		Terrestrial pole	$\Delta$ UT1	Length of day (LOD)	Nutation parameters	Origin	Scale
<b>VLBI</b>	X	X	X	X	X		X
<b>SLR</b>	X	X		X		X	X
<b>GNSS</b>	X	X		X			
<b>DORIS</b>	X	X		X			

- Station coordinates and EOP benefit from a combination
- Origin and scale of ITRF are given by techniques which are able to realize these parameters with high accuracy

→ **Combination leads to higher accuracy and reliability of the products**

# Least squares adjustment: the Gauß-Markov-Model

## Basics

### Observation equation (linear)

- The expected values of the observations  $\mathbf{b}$  are written as a linear combination of known coefficients and unknown parameters  $\mathbf{p}$
- The relations between observations and parameters are defined by physical or mathematical laws

$$\mathbf{A}\mathbf{x} = \mathbf{b} + \mathbf{v}$$

$\mathbf{A}$   $n \times u$  coefficients matrix

$\mathbf{b}$   $n \times 1$  observation vector

$\mathbf{x}$   $u \times 1$  vector of unknowns

$$\mathbf{x} = \mathbf{p} - \mathbf{p}_0$$

$\mathbf{p}$   $u \times 1$  parameter vector

$\mathbf{p}_0$   $u \times 1$  vector of a priori values of  $\mathbf{p}$

$\mathbf{v}$   $n \times 1$  vector of observation errors

# Least squares adjustment: the Gauß-Markov-Model Basics

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Assumption: variance-covariance matrix  $\mathbf{C}_{bb}$  of observations is known, except of a variance factor  $\sigma^2$

$$\mathbf{C}_{bb} = \sigma^2 \mathbf{P}_{bb}^{-1}$$

$\mathbf{P}_{bb}$   $n \times n$  weighting matrix of observations

$$E(\mathbf{v}) = \mathbf{0}$$

$\hat{\mathbf{x}}$  is estimated by applying the condition:  $\hat{\mathbf{v}}^T \mathbf{P}_{bb} \hat{\mathbf{v}} \doteq \text{Min.}$

# Least squares adjustment: the Gauß-Markov-Model

## Basics

### Observation equation (linear)

deterministic part of GMM

$$A\mathbf{x} = \mathbf{b} + \mathbf{v}$$

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stochastic part of GMM

$$\mathbf{C}_{bb} = \sigma^2 \mathbf{P}_{bb}^{-1}$$

$\mathbf{P}_{bb}$   $n \times n$  weighting matrix of observations

$$E(\mathbf{v}) = \mathbf{0}$$

$\hat{\mathbf{x}}$  is estimated by applying the condition:  $\hat{\mathbf{v}}^T \mathbf{P}_{bb} \hat{\mathbf{v}} \doteq \text{Min.}$

# Least squares adjustment: the Gauß-Markov-Model Basics

## Normal equation

$$(A^T P A) \hat{x} = A^T P b \quad \text{with} \quad N = A^T P A \quad \text{and} \\ y = A^T P b$$

$$N \hat{x} = y$$

## Solution

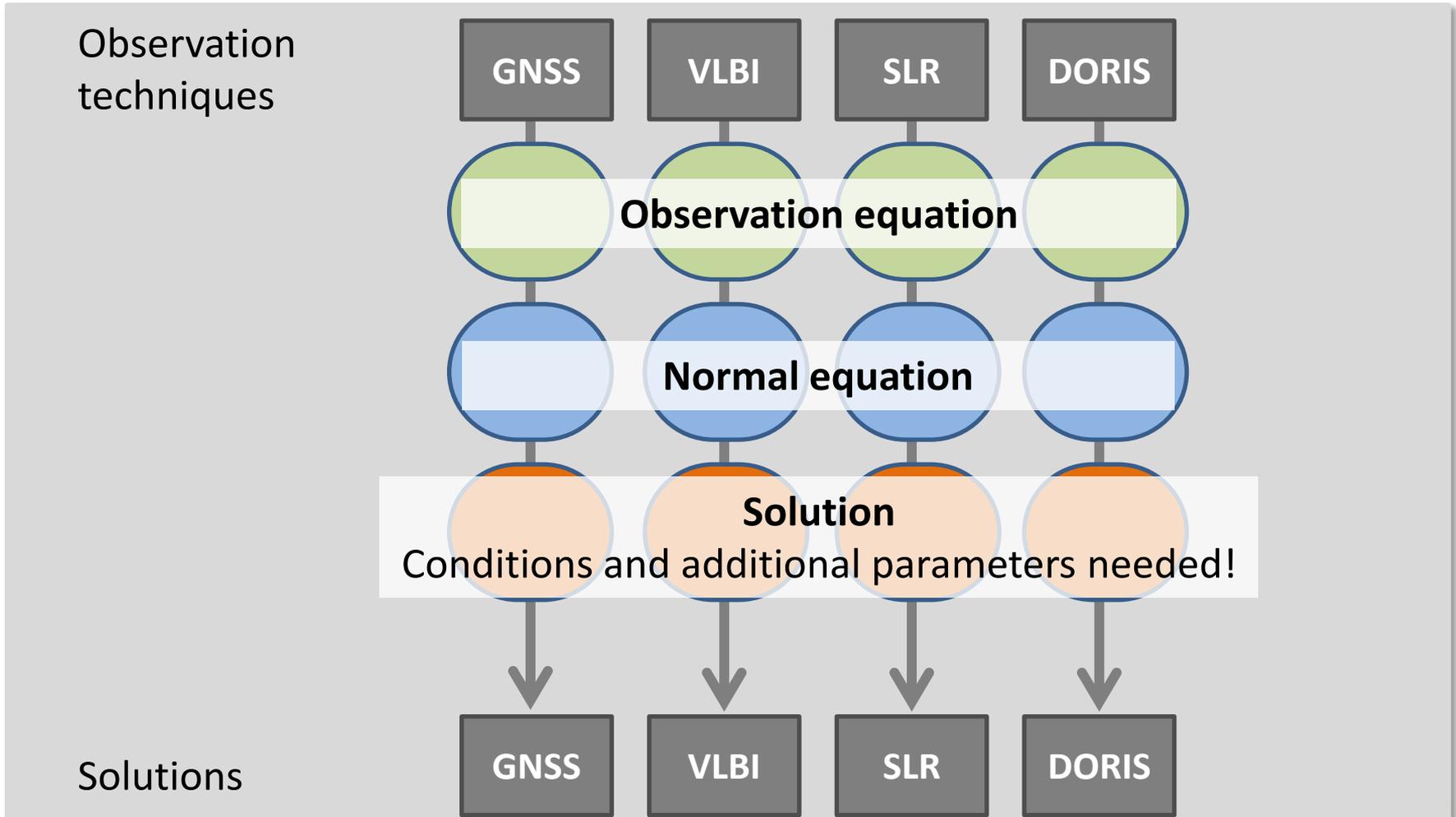
$$\hat{x} = N^{-1} y \quad \text{deterministic part}$$

$$\left. \begin{aligned} \sigma^2 &= (\hat{v}^T P \hat{v}) / (n - u) \\ C_{\hat{x} \hat{x}} &= \sigma^2 N^{-1} \end{aligned} \right\} \text{stochastic part}$$

wherein  $C_{\hat{x} \hat{x}}$  is the variance-covariance matrix of the estimated unknowns  $\hat{x}$

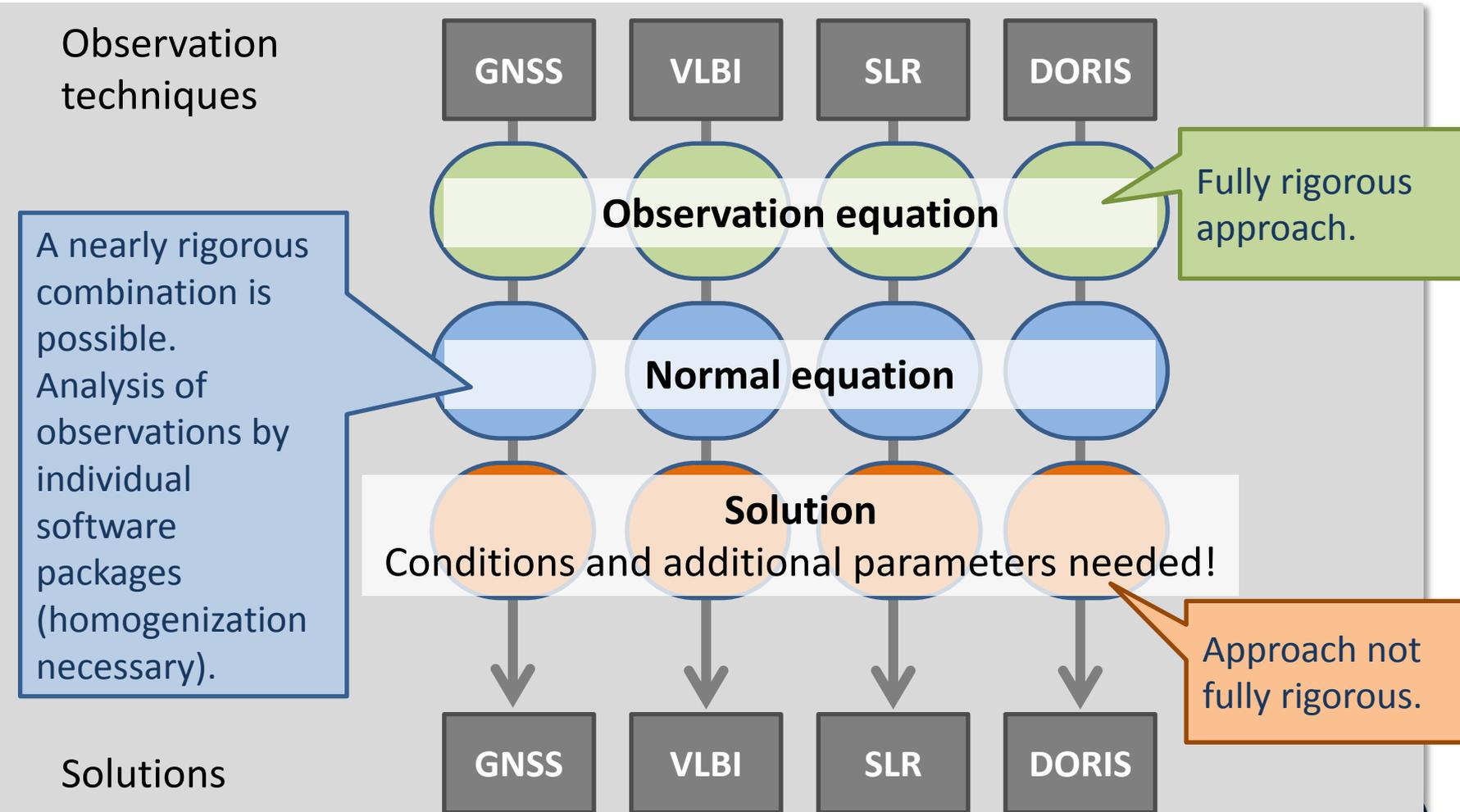
# Conceivable combination approaches

## Combination is possible at the three levels of Gauß-Markov-Model



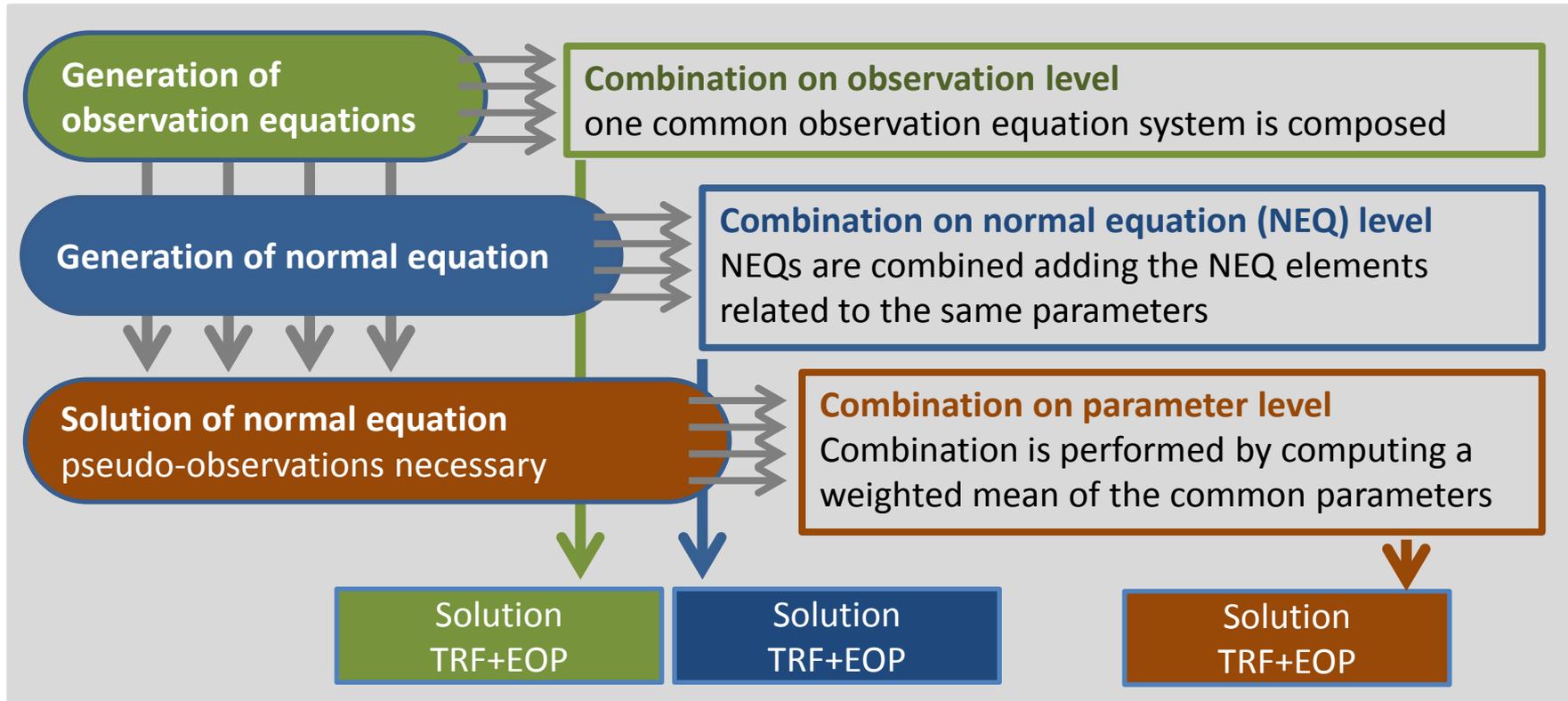
# Conceivable combination approaches

## Combination is possible at the three levels of Gauß-Markov-Model



# Conceivable combination approaches

Prerequisite: different observation techniques provide common parameters



# Conceivable combination approaches

## Application of combination approaches in TRF computation

### Combination at observation level:

Different groups work on software packages able to process and combine all four techniques starting from observation level → not yet fully tested and applied for ITRS realization applications (introduced shortly on the next slides)

### Combination at normal equation level:

ITRS realization DTRF2008 of DGFI (explained in detail later)

### Combination at parameter (solution) level:

Computation of ITRS realization ITRF2008 and previous ITRF solutions of IGN (see the next slides)

# Combination at the observation level

## Observation equation

$$A_k x_k = b_k + v_k$$

$$C_{b_k b_k} = \sigma^2 P_k^{-1}$$

$k = 1, \dots, m$  observation techniques

## Combination on **observation level**

$$\begin{bmatrix} A_1 \\ \dots \\ A_m \end{bmatrix} x = \begin{bmatrix} b_1 \\ \dots \\ b_m \end{bmatrix} + \begin{bmatrix} v_1 \\ \dots \\ v_m \end{bmatrix}$$

$$C_{bb} = \sigma^2 \begin{bmatrix} P_1^{-1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \ddots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & P_m^{-1} \end{bmatrix}$$

Generation of NEQ

Solution of NEQ  
pseudo-observations  
are necessary

Solution  
TRF+EOP



# Combination at the observation level

- Advantages compared to combination of normal equations:
  - A homogeneous analysis of the different observation types by applying the same models and parameterizations is performed innately and must not be organized for different software packages.
  - The pre-processing, i.e. the outlier detection and the weighting of individual observations, is done on the basis of all observations not technique-wise. However, it can be assumed that the impact on the combined solution is quite small.
- The approach is not applied for ITRS realization yet.

# Combination of parameters (IGN approach)

## Parameter (solution) level

Observation equation for the combination on parameter level

$$\mathbf{I} \mathbf{x}_k = \hat{\mathbf{x}} + \mathbf{v}_k$$

$$\mathbf{C}_{\hat{\mathbf{x}}_k \hat{\mathbf{x}}_k} = \sigma^2 (\mathbf{N}_k + \mathbf{D}_k)^{-1}$$

$k = 1, \dots, m$  obs. techn.

$\mathbf{D}$ : NEQ matrix of pseudo observations

→ observations are the solved parameters of input solutions

## Combination on **parameter level**

$$\mathbf{I} \begin{bmatrix} \mathbf{x}_1 \\ \dots \\ \mathbf{x}_m \end{bmatrix} = [\hat{\mathbf{x}}] + \begin{bmatrix} \mathbf{v}_1 \\ \dots \\ \mathbf{v}_m \end{bmatrix}$$

$$\mathbf{C}_{xx} = \sigma^2 \begin{bmatrix} (\mathbf{N}_1 + \mathbf{D}_1)^{-1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \ddots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & (\mathbf{N}_m + \mathbf{D}_m)^{-1} \end{bmatrix}$$



Solution  
TRF+EOP

# Combination of parameters (IGN approach)

- In order to realize the geodetic datum while generating the input solutions, pseudo-observations are applied ( $\hat{\mathbf{x}}_k = \mathbf{D}^{-1}\mathbf{d}$ ). → The resulting variance-covariance matrix used as weighting matrix in the combination depend on the used conditions.

$$\hat{\mathbf{x}}_k = (\mathbf{N} + \mathbf{D})^{-1}(\mathbf{y} + \mathbf{d})$$
$$\mathbf{C}_{\hat{\mathbf{x}}_k\hat{\mathbf{x}}_k} = \sigma^2(\mathbf{N}_k + \mathbf{D}_k)^{-1}$$

- Usually applied conditions are
  - No-Net-Translation (NNT) and No-Net-Rotation (NNR) conditions which do not allow a translation and a rotation of the solved station network w.r.t. the a priori coordinates.
  - Loose constraints: a slightly constraining of all station coordinates to their a priori values.

# Combination of parameters (IGN approach)

- In the combination, singularity of the individual input solutions w.r.t. datum parameters is rebuilt by setting up parameters of a Helmert transformation (3 translations, 3 rotations, scale) → necessary, because datum realization has to be redone homogeneously for the ITRF solution. E.g. for technique  $k$  the observation equation (see previous slide) is extended by the equation of Helmert transformation:

$$\hat{\boldsymbol{x}} = \boldsymbol{x}_k + \boldsymbol{T}_k + D_k \boldsymbol{x}_k + \boldsymbol{R}_k \boldsymbol{x}_k$$

**$T$** : Translation matrix  
 **$R$** : Rotation matrix  
 **$D$** : Scale factor

A set of good and global distributed stations is used to determine the transformation parameters.

# Combination of parameters (IGN approach)

- This approach is not fully rigorous mainly because:
    - The weights of the input parameters are not independent from the datum realization of the input solutions. In particular in case of applied loose constraints, the variances are not reliable.
    - The Helmert transformation parameters and thus the solution strongly depend on the selected set of stations used for the transformation.
- 

## References for the IGN approach, e.g.:

Altamimi et al. 2011

IERS Conventions 2010

# Combination of normal equations (DGFI approach)

## Observation and Normal equation

Observation equation

$$A_k \mathbf{x}_k = \mathbf{b}_k + \mathbf{v}_k$$

$k = 1, \dots, m$  techniques

$$C_{b_k b_k} = \sigma^2 P_k^{-1}$$



Normal equation

$$N_k \hat{\mathbf{x}}_k = \mathbf{y}_k$$

with:  $N = A^T P A$  and  
 $\mathbf{y} = A^T P \mathbf{b}$

## Combination at the normal equation level

$$N = \frac{1}{\sigma_1^2} N_1 + \dots + \frac{1}{\sigma_m^2} N_m \quad N_{u \times u}$$

$$\mathbf{y} = \frac{1}{\sigma_1^2} \mathbf{y}_1 + \dots + \frac{1}{\sigma_m^2} \mathbf{y}_m \quad \mathbf{y}_{u \times 1}$$

$$\mathbf{b}^T P \mathbf{b} = \frac{1}{\sigma_1^2} \mathbf{b}_1^T P_1 \mathbf{b}_1 + \dots + \frac{1}{\sigma_m^2} \mathbf{b}_m^T P_m \mathbf{b}_m$$

Solution of NEQ

TRF + EOP

# Solution of combined normal equation (DGFI)

Parameter (deterministic part)

$$\hat{\mathbf{x}} = \mathbf{N}^{-1}\mathbf{y}$$

Variance-covariance matrix of the parameters  $\mathbf{C}_{\hat{\mathbf{x}}\hat{\mathbf{x}}}$  (stochastic part)

$$\sigma^2 = (\hat{\mathbf{v}}^T \mathbf{P} \hat{\mathbf{v}}) / (n - u)$$

$$\text{with } \hat{\mathbf{v}}^T \mathbf{P} \hat{\mathbf{v}} = \hat{\mathbf{b}}^T \mathbf{P} \hat{\mathbf{b}} - \mathbf{y}^T \hat{\mathbf{x}}$$

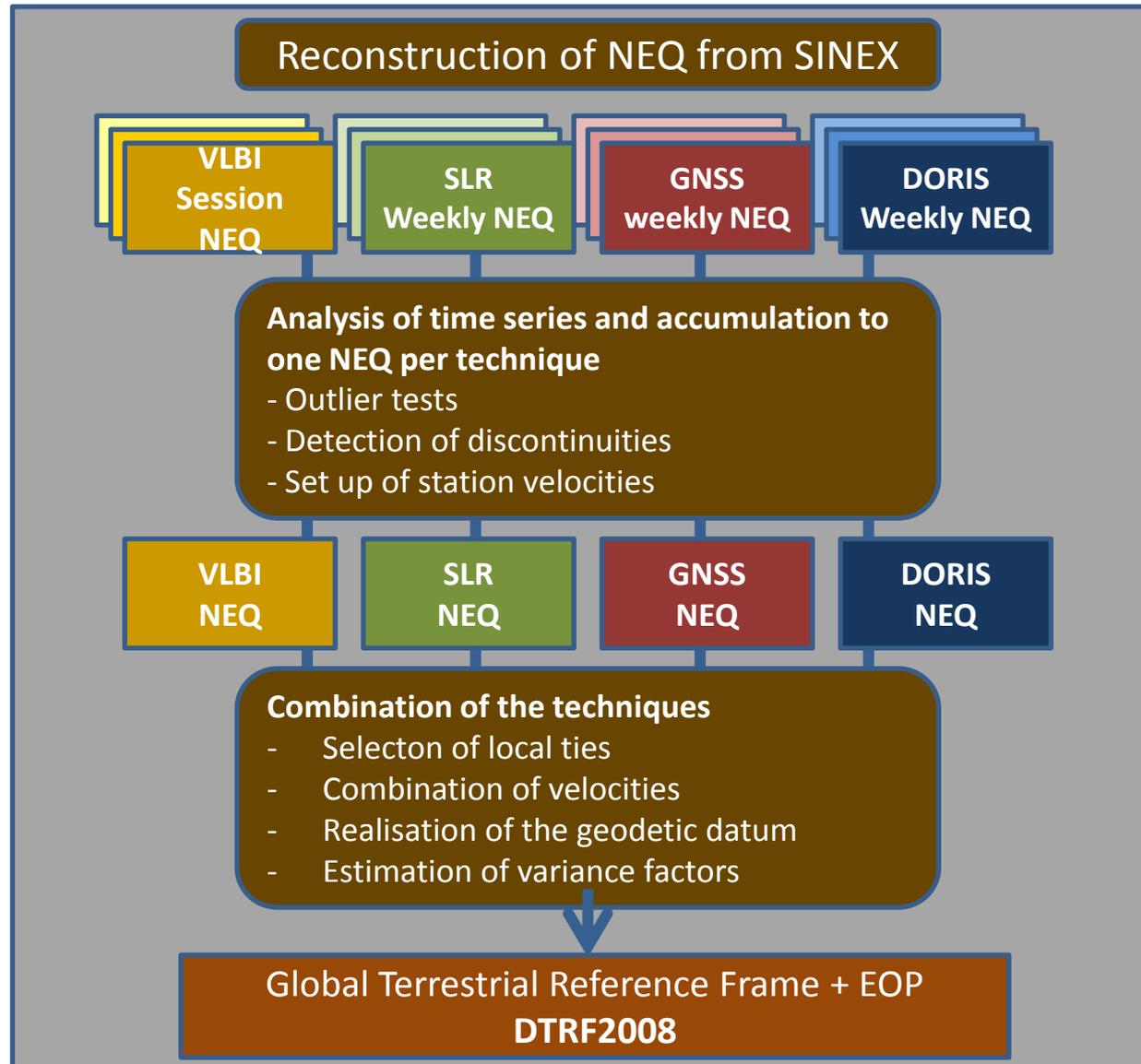
$$\mathbf{C}_{\hat{\mathbf{x}}\hat{\mathbf{x}}} = \sigma^2 \mathbf{N}^{-1}$$

---

Note: Input data are normal equations, which are constraint free w.r.t. those geodetic datum parameters they are not sensitive for! But constraints necessary in order to stabilize certain groups of weak parameters (e.g. clock or troposphere parameters) are included.

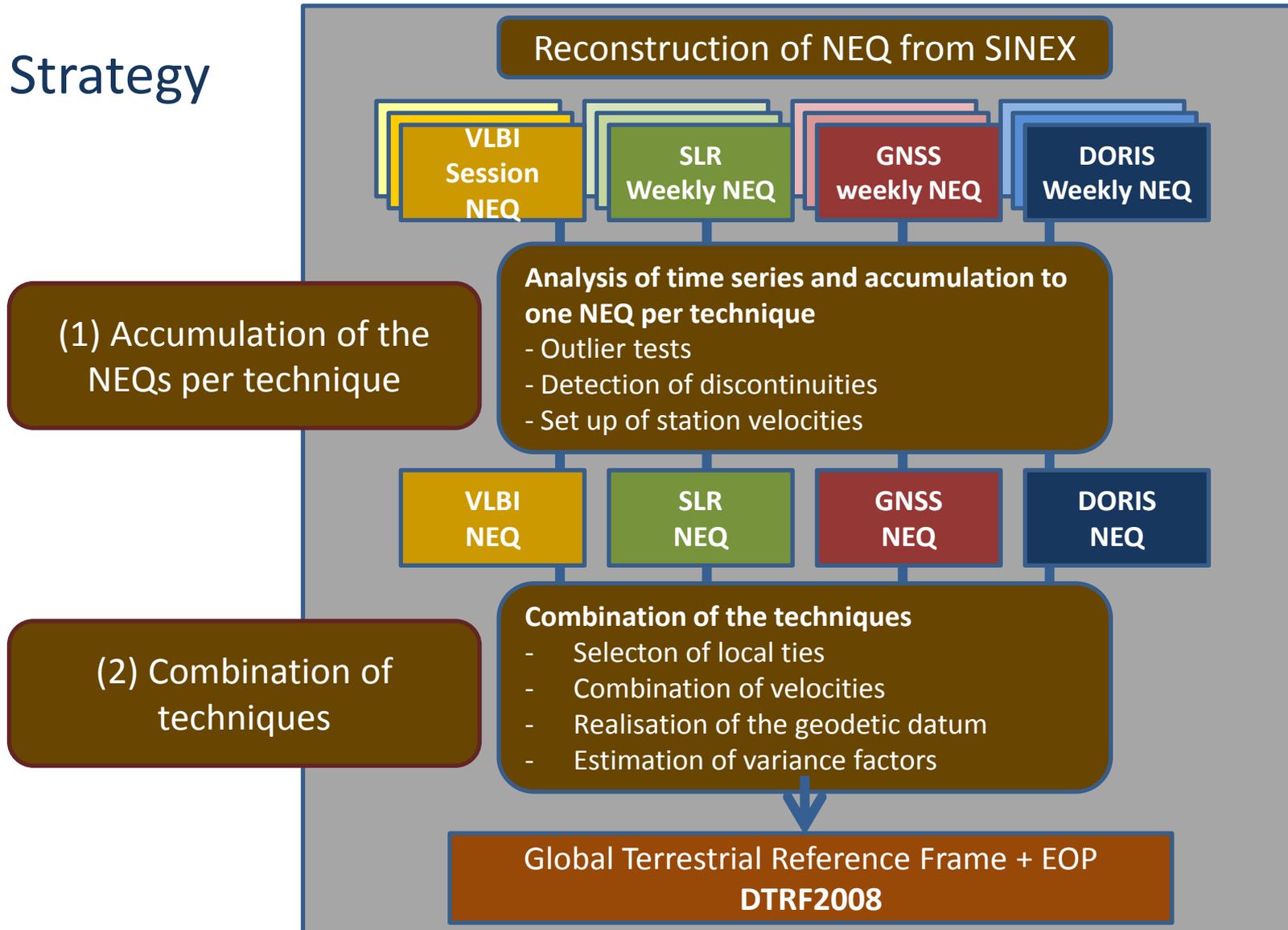
# Computation of DGFI solution DTRF2008

## Strategy



# Computation of DGFI solution DTRF2008

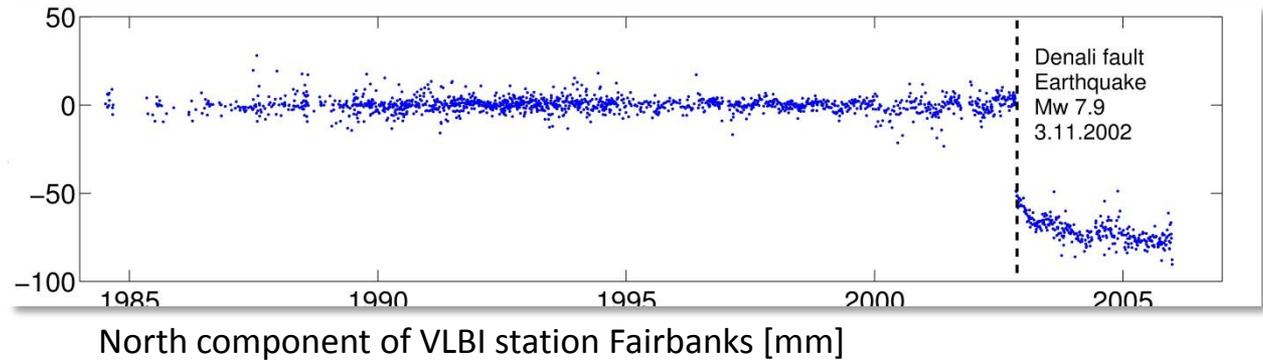
## Strategy



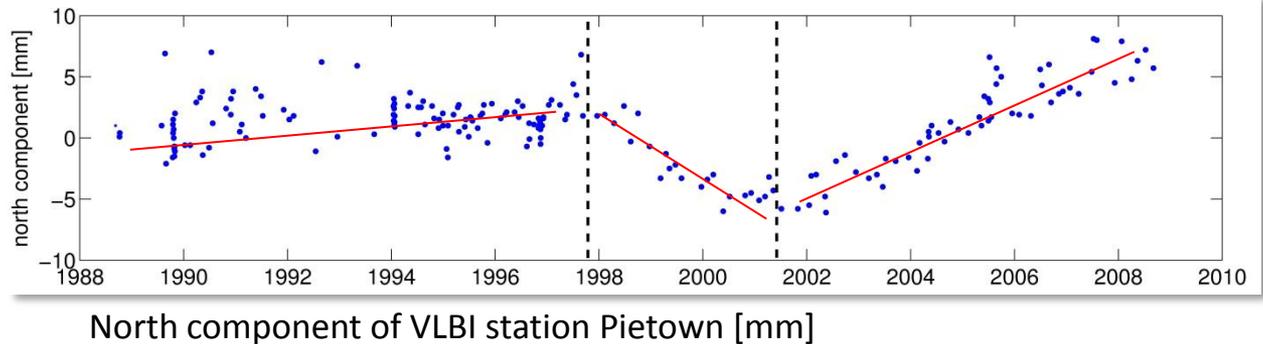
# Time series analysis ...

## ... for discontinuity detection

Discontinuity in the station movement due to an earthquake



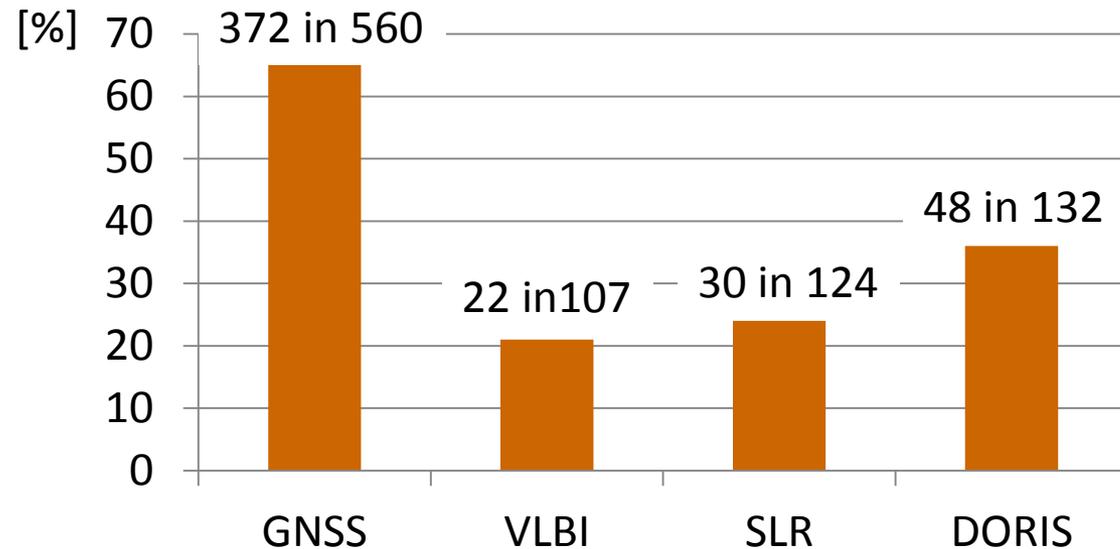
Discontinuity of station velocity



# Time series analysis ...

## ... for discontinuity detection

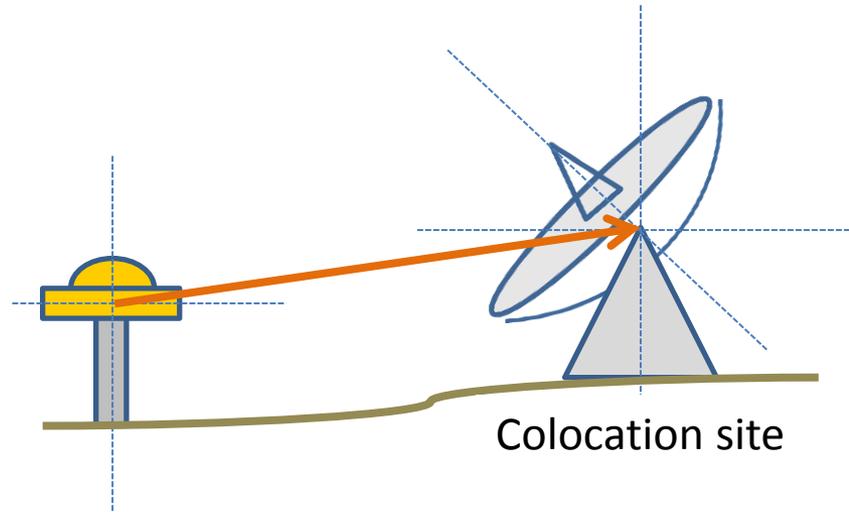
*Number of stations affected by discontinuities in DTRF2008*



Many GNSS stations are affected by discontinuities. In many cases, it can be related to equipment changes! A monitoring of these changes would help to reduce the number of discontinuities significantly.

# Colocation sites

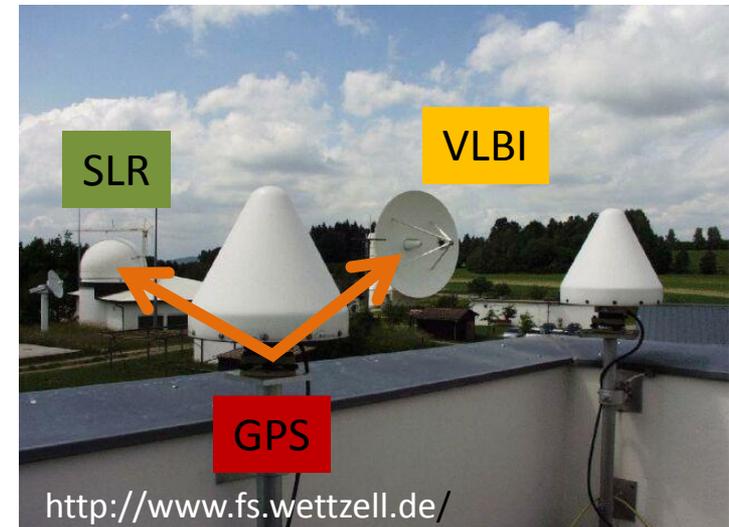
Observations of different space geodetic techniques do usually not refer to common reference points



Difference measurements (terrestrial, GPS) are necessary for the combination of station positions.

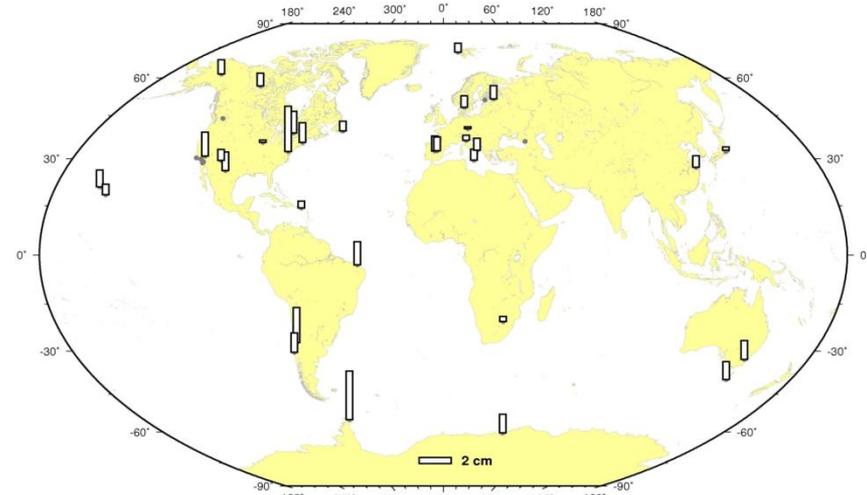
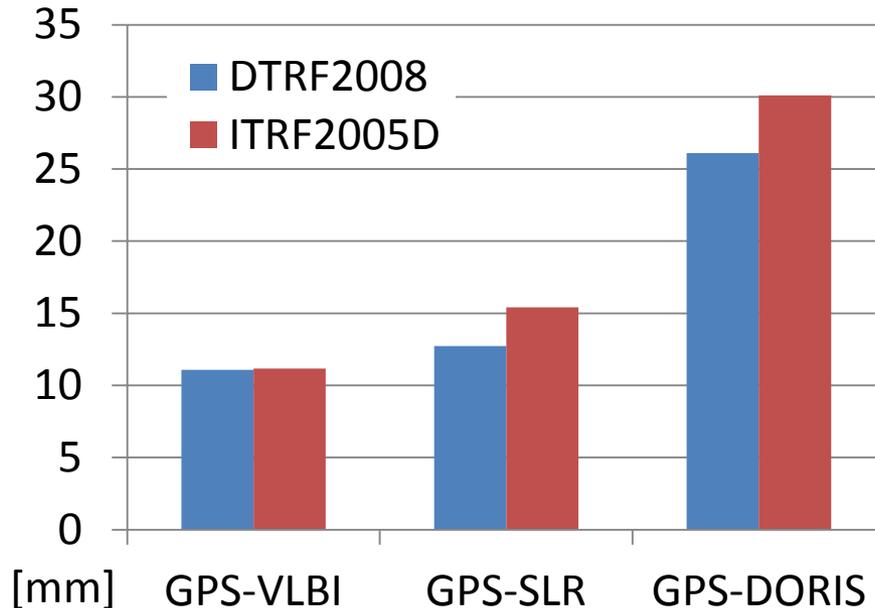
The difference vectors are named as „local ties“. Problem: They show large discrepancies w.r.t. the geodetic space techniques (some centimetres) at some sites. → the handling of local ties in ITRS realization is difficult.

Geodetic observatory Wettzell,  
Bavarian Forest



# Colocation sites

## Local tie misfits from DTRF2008 computation (3-dimensional)

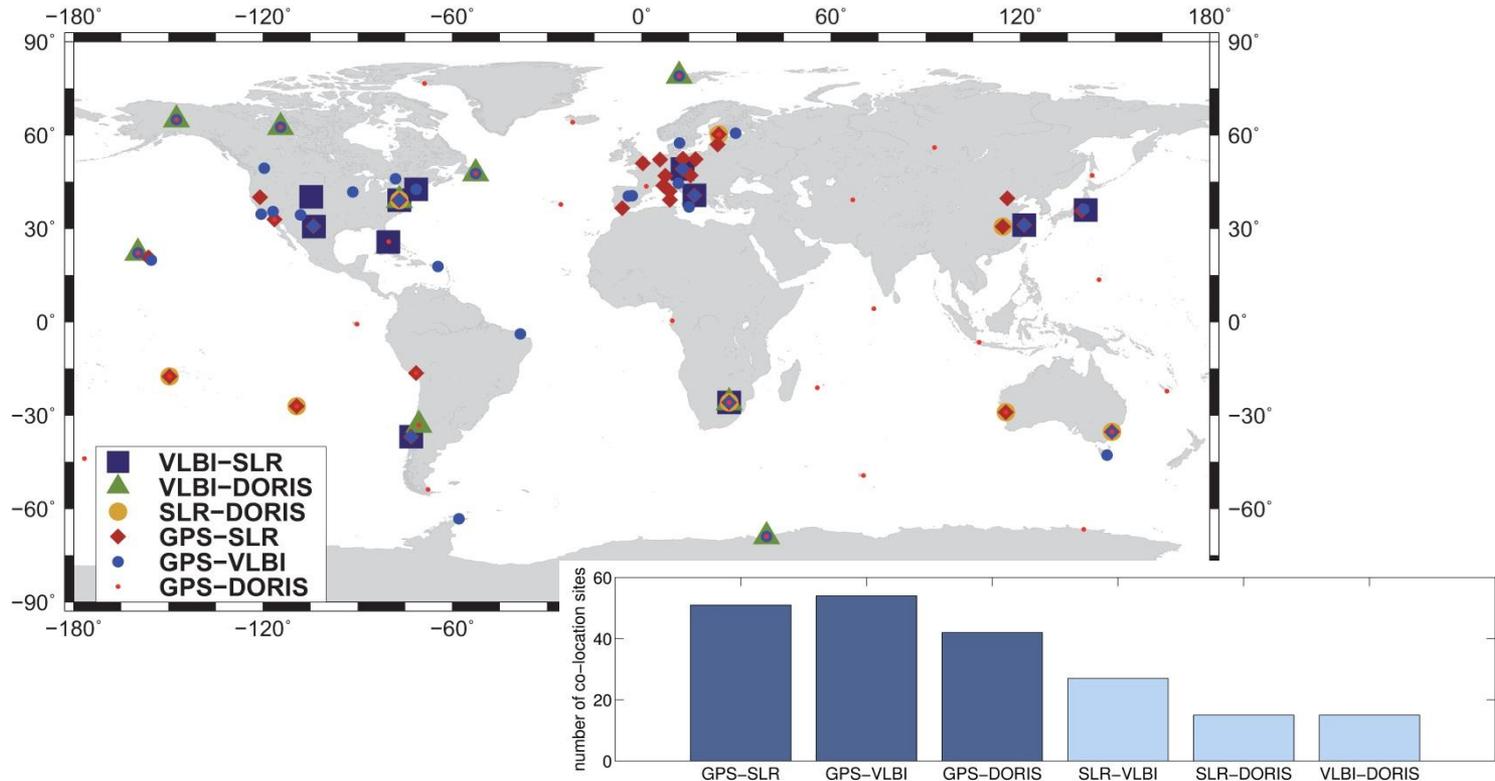


VLBI-GNSS colocation sites  
(DTRF2008 computation)

- Reasons: model deficiencies (space techniques) or local tie measurement errors
- Improvement w.r.t. ITRF2005 due to model improvements.
- But, local tie misfits reach still centimetres.
- VLBI-GNSS sites show the smallest discrepancies. For some stations even less than 5mm.

# Global distribution of collocation sites

## Collocation sites used in DTRF2008



GNSS contributes to most of the collocations. → GNSS is fundamental for the combination of all station networks on a high accuracy level.

# Colocation sites and EOP

**Combination of station coordinates** provides one station network with

- One origin
  - One orientation
  - One scale
- }  $\pm$  uncertainty of realization

**The combination of the EOP** (pole coordinates) combines the orientation of the technique-specific networks (w.r.t. x and y axis)

→ Both ways must be consistent



**Pole coordinates are used for the validation of the local ties:** local ties and their standard deviations are chosen claiming

- that the offsets between the (still uncombined) pole coordinates are minimal
  - that the deformation of the networks due to the combination is minimal
- The two conditions are contrary and the introduction of local ties a complex process

# Realisation of the geodetic datum ...

## ... in accordance to the ITRS definition in the IERS Conventions

- Origin** realized from SLR observations (VLBI not sensitive, GNSS and DORIS are affected by systematics)
- Scale** realized from SLR and VLBI (GNSS and DORIS are affected by systematics)
- Orientation** „no-net-rotation“ conditions w.r.t. ITRF2005 using a subset of GNSS stations (high accuracy, well globally distributed)

# Conditions in the Gauß-Markov model

## Solution

Because of the rank deficiency of  $\mathbf{N}$ , pseudo observations must be added

$$\hat{\mathbf{x}} = (\mathbf{N} + \mathbf{D})^{-1}(\mathbf{y} + \mathbf{d})$$

$\mathbf{D}$  is the NEQ matrix and

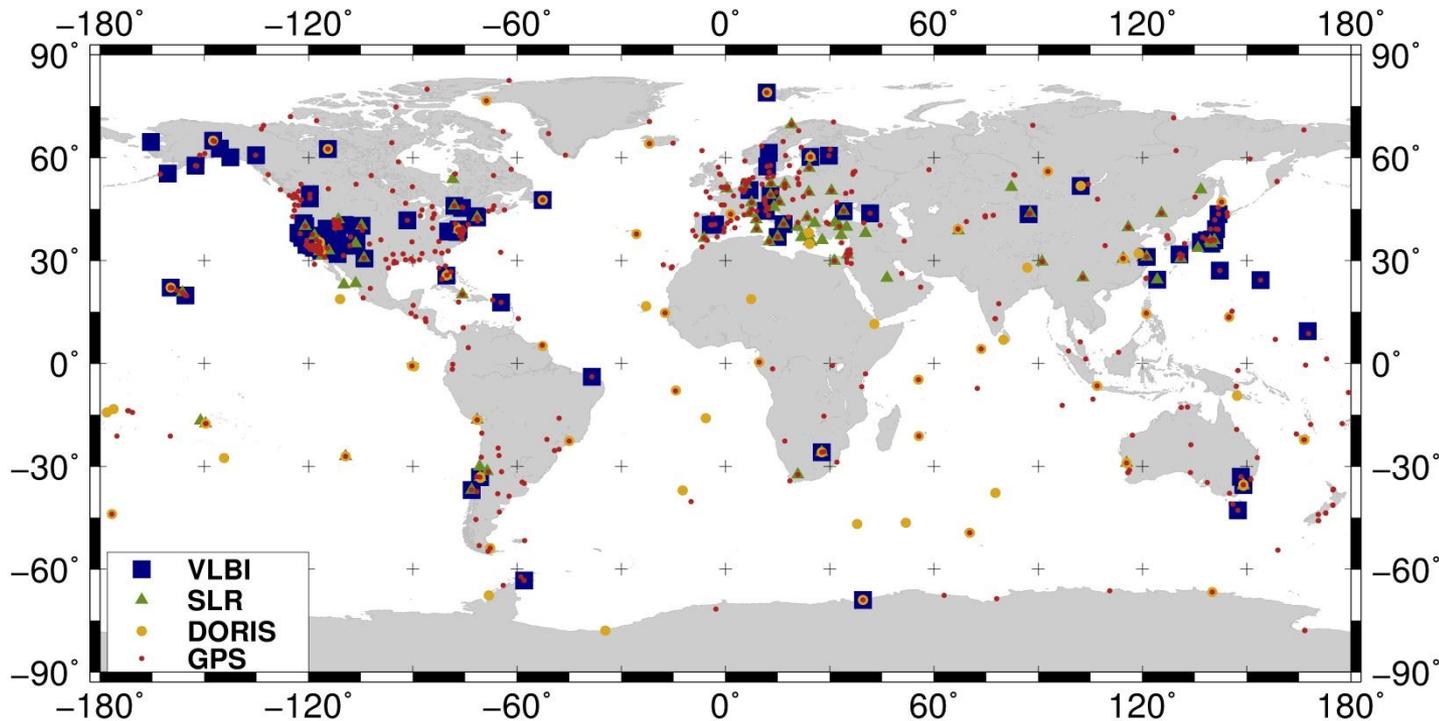
$\mathbf{d}$  the right hand side of normal equation of the conditions

## In ITRS realization,

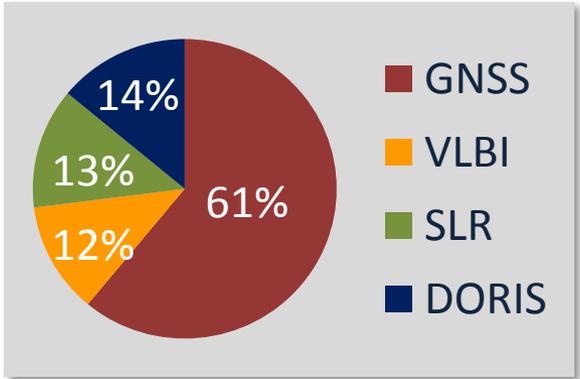
Pseudo-observations are used for the introduction of the local ties and combination of the velocities at colocation sites.

After doing this,  $\mathbf{N}$  has still a rank deficiency with respect to datum parameters of orientation: No-net-rotation conditions are added based on a subset of GPS stations which provide a high accuracy.

# DTRF2008: station distribution



VLBI	106
SLR	122
GNSS	559
DORIS	132
<hr/>	
Total	≈1000



# DTRF2008: station distribution

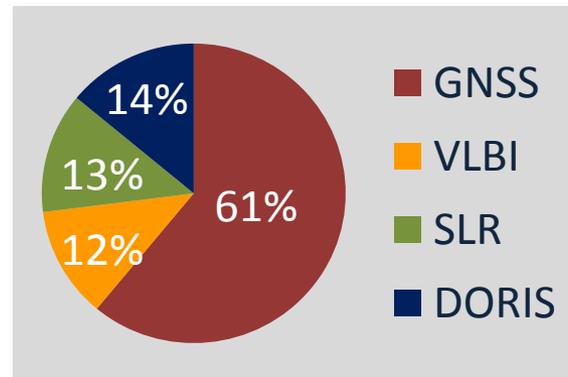
## Discussion:

GNSS dominates the frame and contributes to most of the colocations but many of the GNSS stations are affected by discontinuities (equipment changes).

Furthermore, the GNSS observation time span is more than 10 years shorter as for VLBI and SLR.

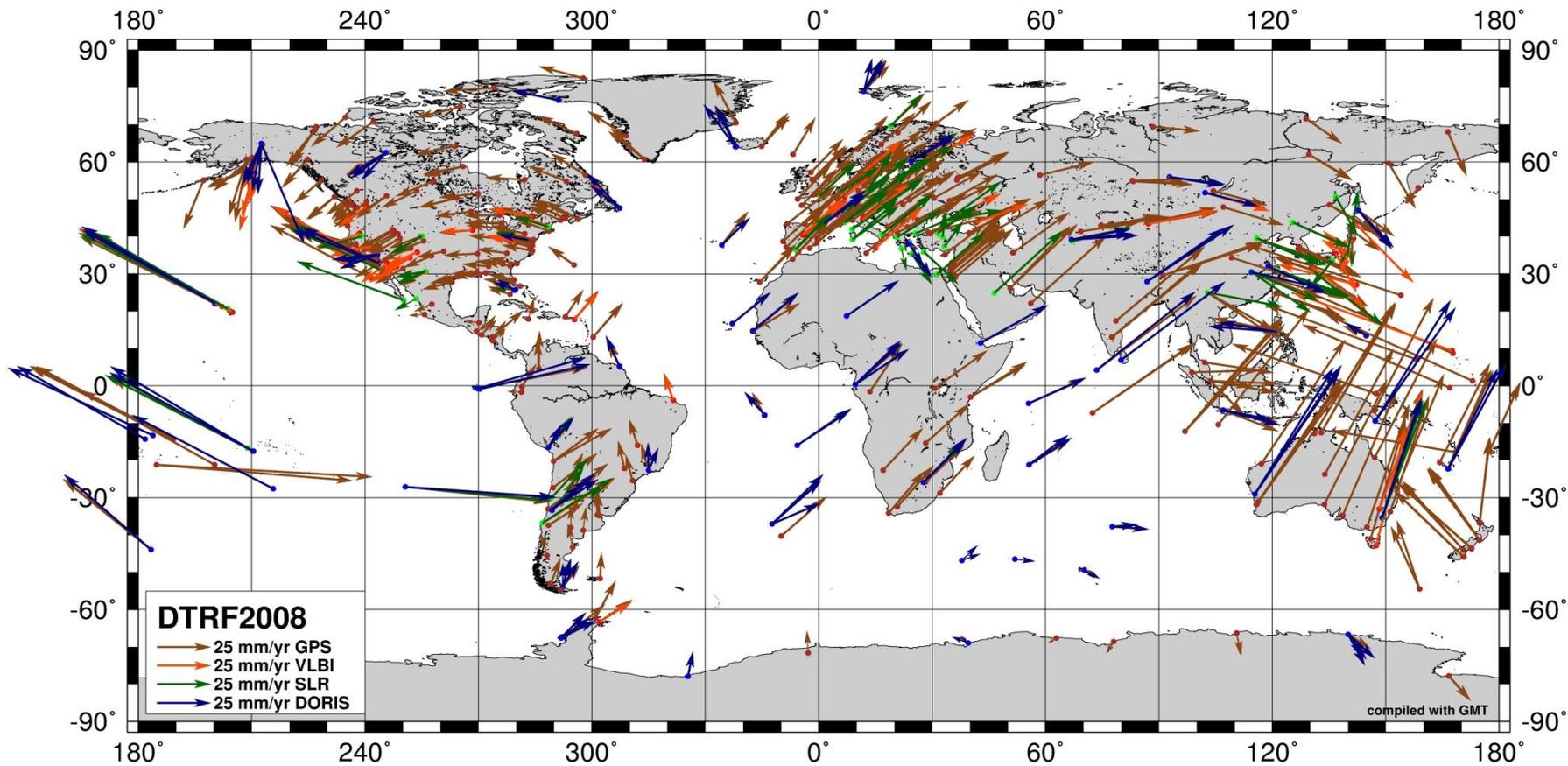
→ A reduction of discontinuities in GNSS time series will lead to a significant improvement of accuracy and long-term stability of the frame.

VLBI	106
SLR	122
GNSS	559
DORIS	132
<hr/>	
Total	≈1000



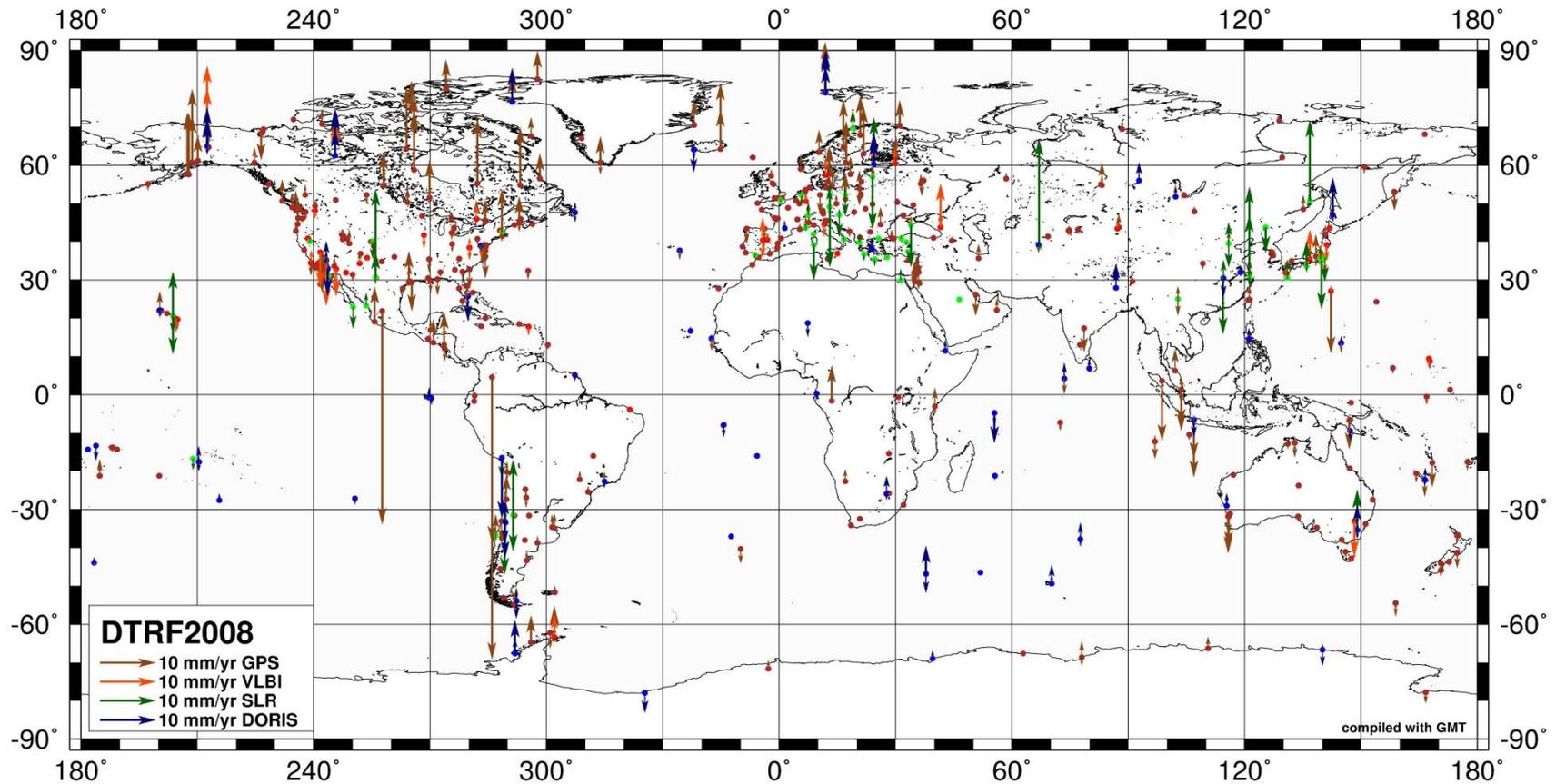
# DTRF2008: velocity field

## Horizontal velocity field of DTRF2008



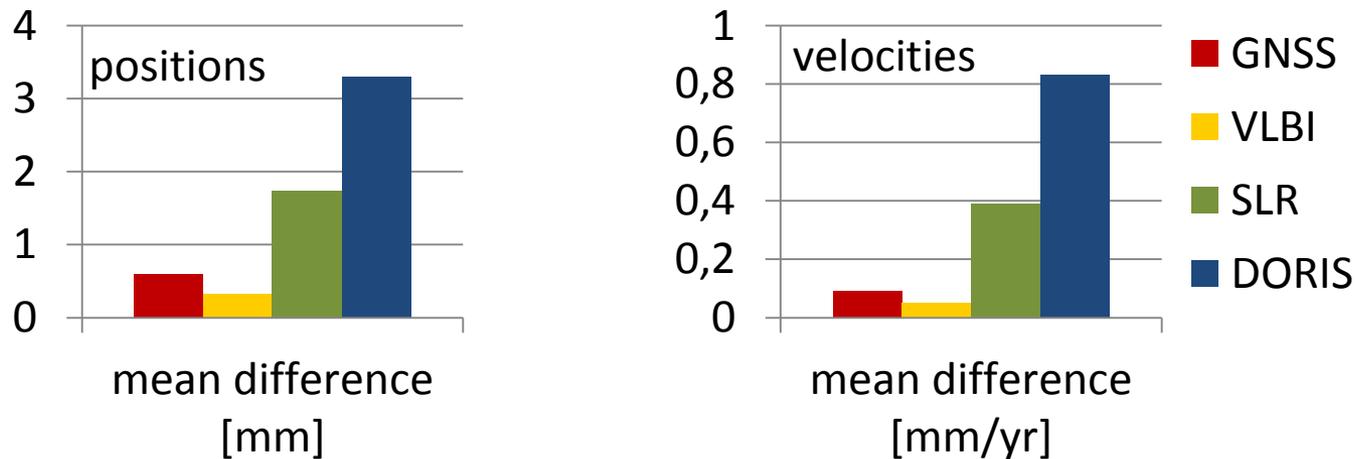
# DTRF2008: velocity field

## Vertical velocity field of DTRF2008



## Internal accuracy

- **Geodetic datum:** within 0.6 mm and 0.1 mm/yr
- **Network geometry** (for good stations):

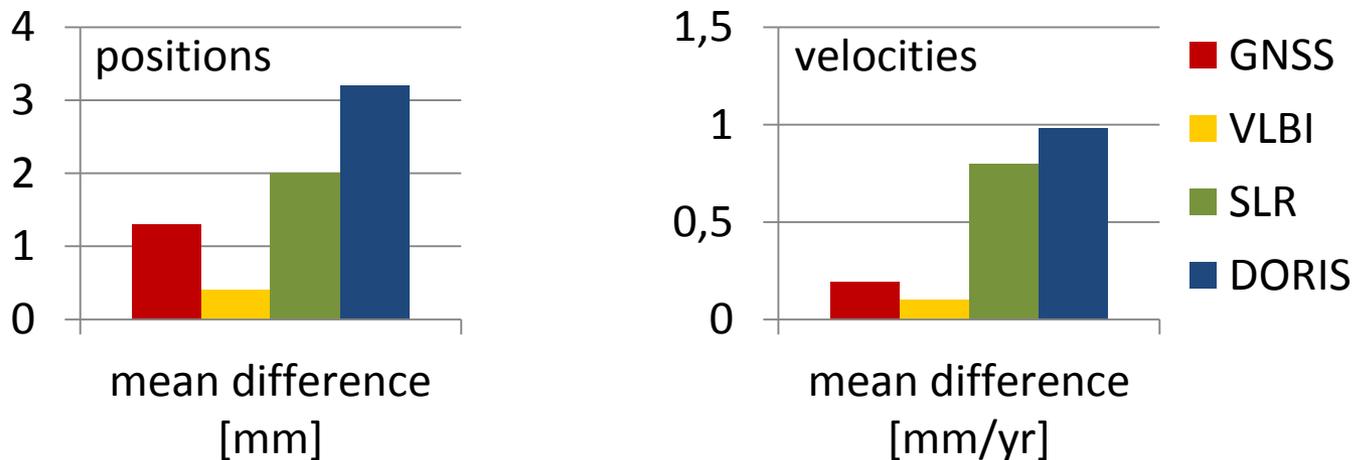


A high internal accuracy is achieved for good stations. For stations with short observation time spans the values can reach centimetres and some mm/yr.

# DTRF2008: external accuracy

## Comparison with ITRF2008 (IGN)

- **Geodetic datum** (origin, orientation, scale):  
Discrepancies  $\leq 6$  mm and  $\leq 0.5$  mm/a
- **Network geometry**  
Subset of good and well distributed stations

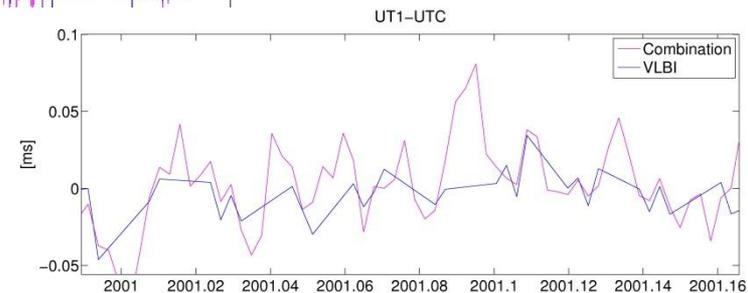
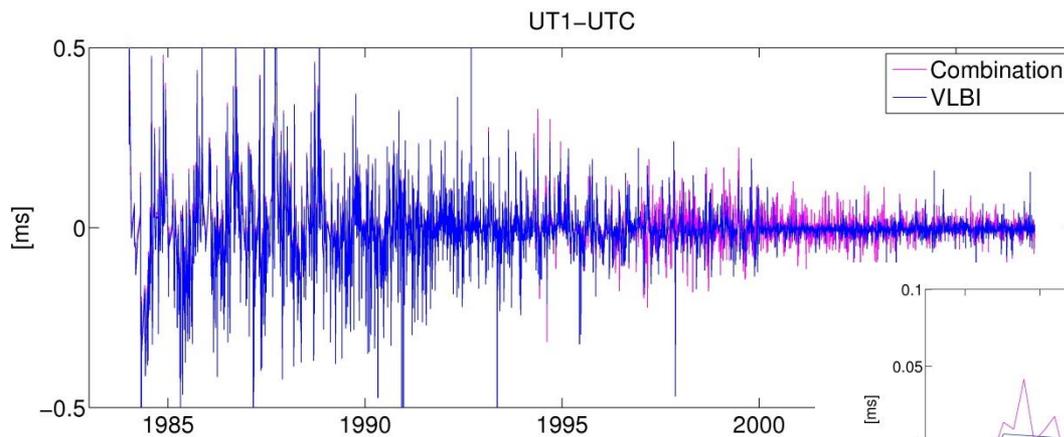
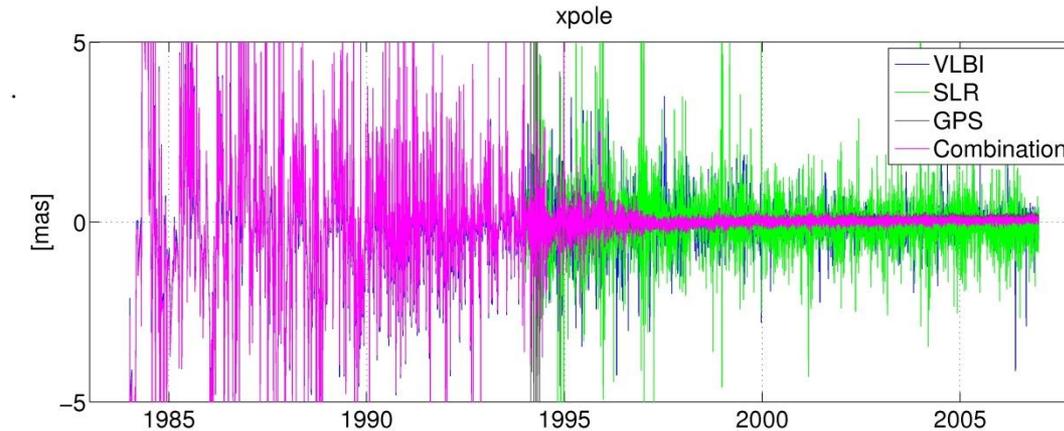


Individual stations: discrepancies of some centimetres.

→ The comparison of TRF solutions shows, that the GGOS requirements [1mm and 0.1 m/yr] (Rothacher et al. 2012) are not yet reached! Further developments are necessary!

# DTRF2008: EOP time series

## EOP with respect to IERS 08 C04



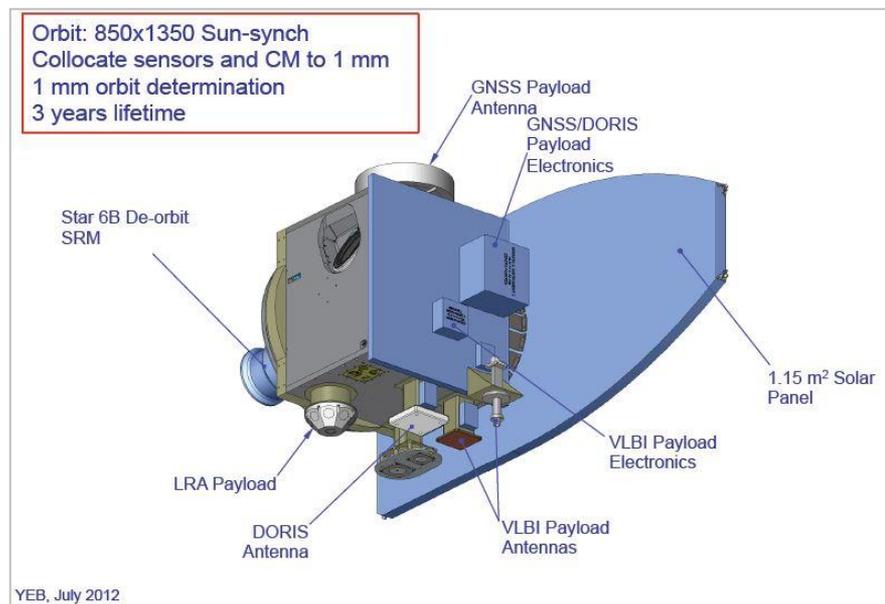
- The scatter is reduced by the combination
- UT1-UTC: from 1997 the time series are continuous, because the available GNSS and SLR rates allow for an interpolation

# Summary TRF

- The combination of the space leads to a TRF solution of high accuracy and long-term stability.
- The individual strengths of the techniques are used for TRF computation. VLBI is unique to link ITRF and ICRF. Furthermore, the accuracy of VLBI stations in ITRF is very high due to long observation time series (about 30 years) and a low number of discontinuities in station position time series.
- Station coordinates and EOP are estimated consistently in one adjustment.
- The agreement of TRFs computed by different ITRF CC is for good stations within 6 mm and 1.5 mm/yr. But for some stations also centimeter differences exist.
- In order to guarantee for a high accuracy of the ITRF a new realization is computed every 3-5 years.

# Summary TRF

- The reduction of discontinuities in GNSS station position time series would lead to a further improvement of the long-term stability.
- A better global distribution of the collocation sites would also lead to a higher accuracy of the TRF.
- Collocation satellites (see e.g. the GRASP proposal by NASA/JPL) are expected to improve the reference frame significantly.



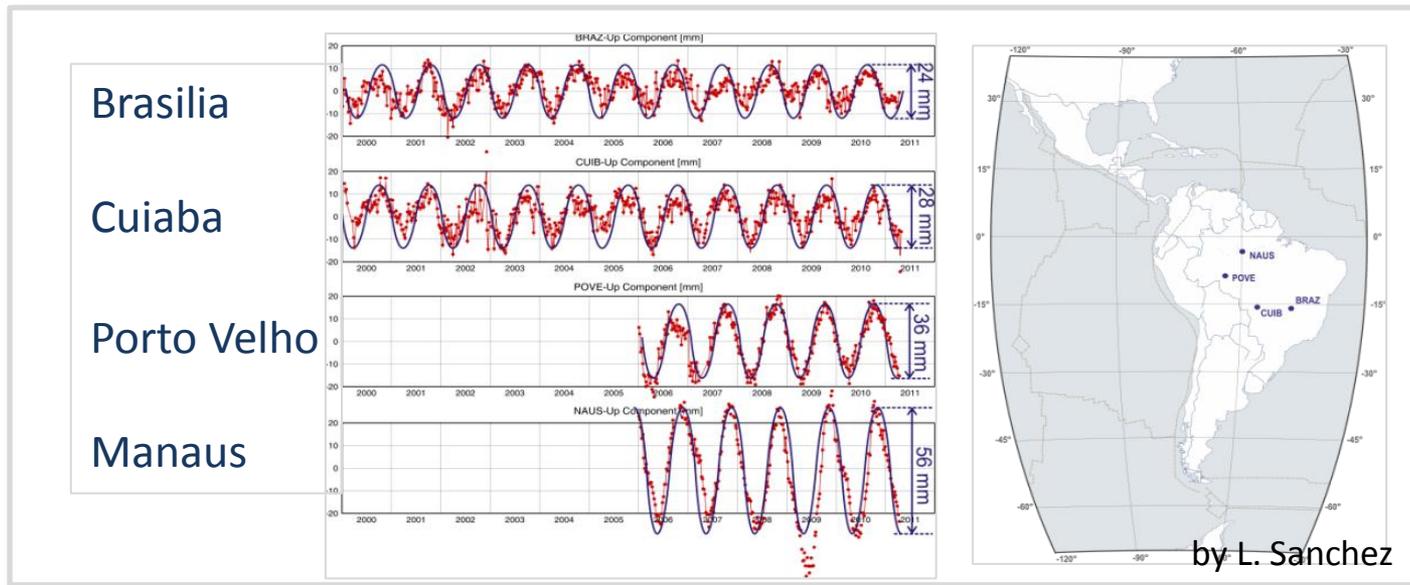
By Bar-Server et al., JPL

## Research topics

- non-linear station movements mainly caused by changes in mass distribution and mass load are not yet considered because the modeling is quite difficult. The station coordinates and consistently estimated parameters can be falsified.
  - The IERS Global Geophysical Fluid Centre is working on models which have a sufficient accuracy.
  - Another idea: time series of epoch reference frames in addition to the ITRF
- ITRF and ICRF and the related EOP are not consistent today as they are computed from different data sets, by different institutions and with different software packages. The International Union of Geodesy and Geophysics (IUGG) adopt a resolution on a consistent realization of both frames and the International Astronomical Union (IAU) established a working group which aims for a ICRF-3 which is consistent to the ITRF.
  - first investigations are performed by DGFI

# Epoch reference frames: Motivation

- Station displacements due to changes of the mass distribution in the Earth system and mass load changes on Earth's crust are not (or not adequately) considered by TRF computation today. This limits their accuracy.
- Epoch-wise (e.g. weekly) estimation of station positions allows for approximating the displacements with high accuracy.



*Examples for large vertical station displacements due to atmospheric and hydrologic mass load changes*

# Epoch reference frames: Strategy

## Weekly combination of space geodetic techniques

Weekly NEQs of  
satellite techniques

NEQ  
GNSS

+

NEQ  
SLR

=

NEQ  
satellite  
techniques

+

Session-wise NEQ  
from VLBI

VLBI-S1

VLBI-S2

=

NEQ  
combined

+

NEQ  
DORIS

VLBI-S..

Final solution  
[pos, EOP]

Epoch  
reference  
frame

- Introduction of local ties
- Realization of the geodetic datum
- Variance component estimation

# Epoch reference frames: Discussion

## Pros

- Approximates the true station movement w.r.t. the center of mass with high accuracy (e.g. the alignment of regional frames would improve significantly)
- Consequently, consistent estimated parameters (e.g. EOP) can not suffer from non-modeled non-linear movements
- Benefits from the combination of the techniques (compared to the single-technique epoch solutions)
- Fast computation to provide new positions is possible (e.g. after earthquakes)

## Cons

- Accuracy is not as high as for the ITRF (low redundancy, lower density of station networks, only a few local ties)
- Low long-term stability
- Dependency from ITRF: alignment w.r.t. frame orientation
- Frames of the early years do not benefit from the high quality of the present observations (compared to ITRF)

# Epoch reference frames: Discussion

## Pros

- Approximates the true station movement w.r.t. the center of mass with high accuracy (e.g. the alignment of regional frames would improve significantly)
- Consequently, consistent estimated parameters (e.g. EOP) can not suffer

### Conclusion:

Epoch reference frames will become more important in future, but more investigations are necessary to improve their stability.

Accuracy is not as high as for the ITRF (low redundancy, lower density of station networks, only a few local ties)

- Low long-term stability
- Dependency from ITRF: alignment w.r.t. frame orientation
- Frames of the early years do not benefit from the high quality of the present observations (compared to ITRF)

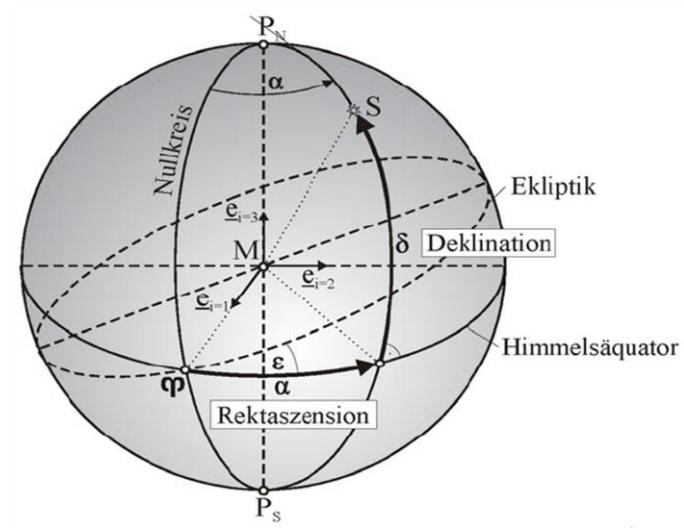
# The Terrestrial and the Celestial Reference Frame

- How they are related?
- How consistent they are?

# Celestial Reference System (ICRS)

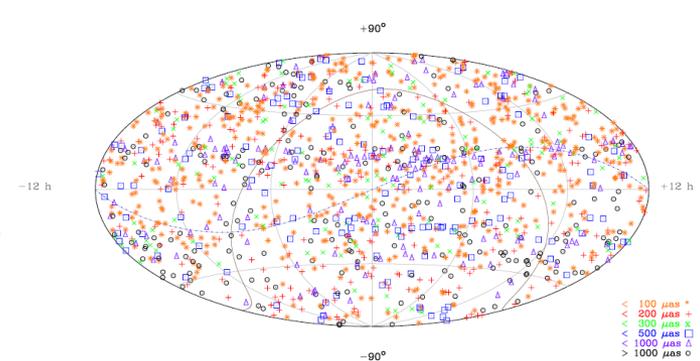
## Definition

- The origin  $M$  is located in the barycentre of the solar system
- The  $\underline{e}_3$  axis is the mean Earth rotation axis
- The  $\underline{e}_1$  and  $\underline{e}_2$  axis lie within the plane of the mean celestial equator of epoch J2000.0
- The  $\underline{e}_1$  axis is directed to the point of the Vernal equinox  $\Upsilon$

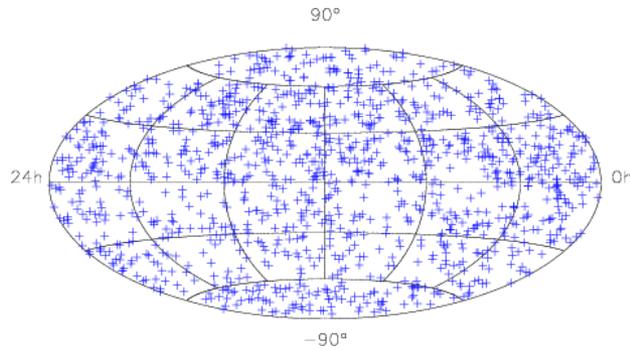


## Realization (ICRF)

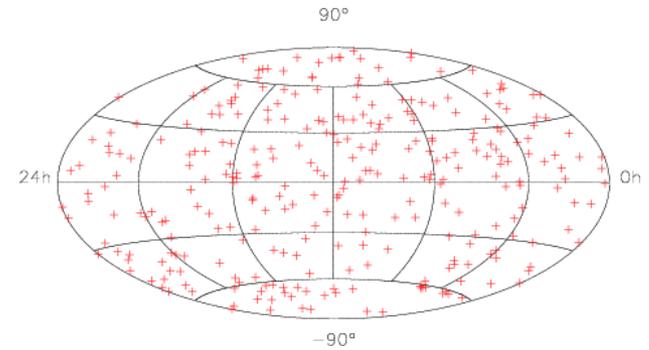
- Coordinates  $(\alpha, \delta)$  of radio sources
- Only sources with a high accurate position are used for the definition of the axes



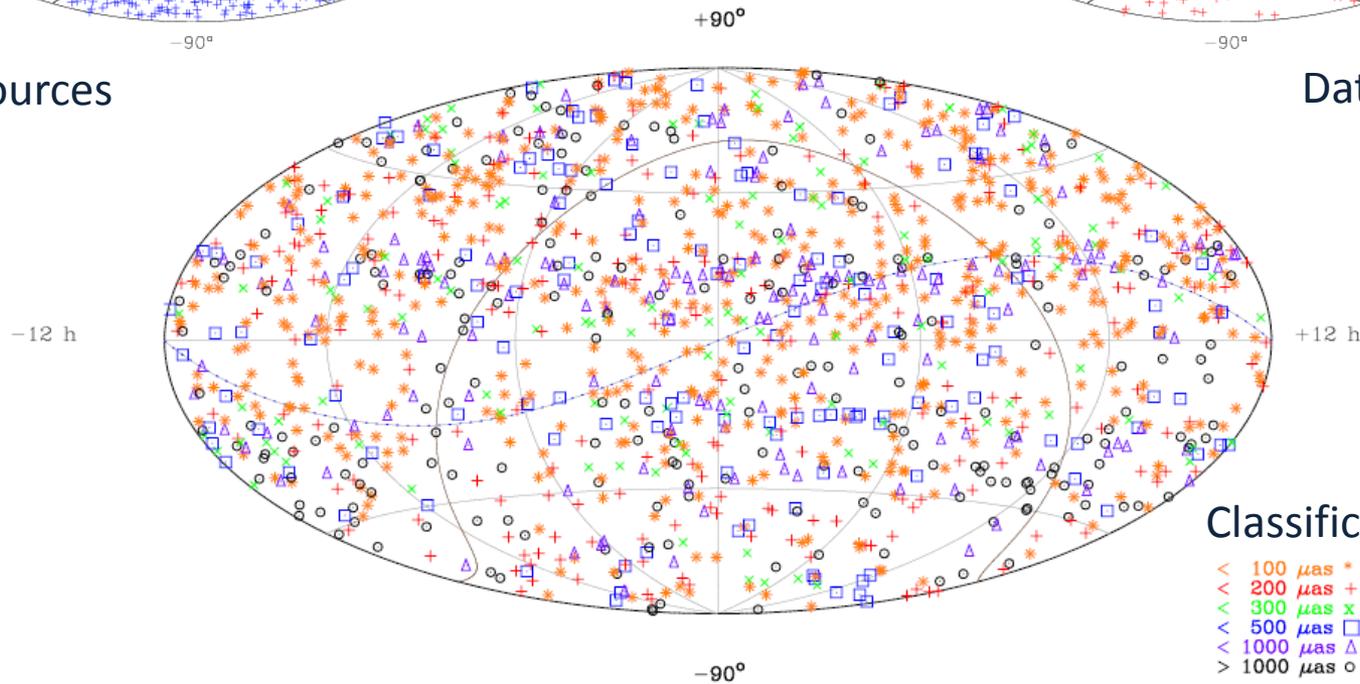
# Celestial Reference System (ICRS)



All sources



Datum sources



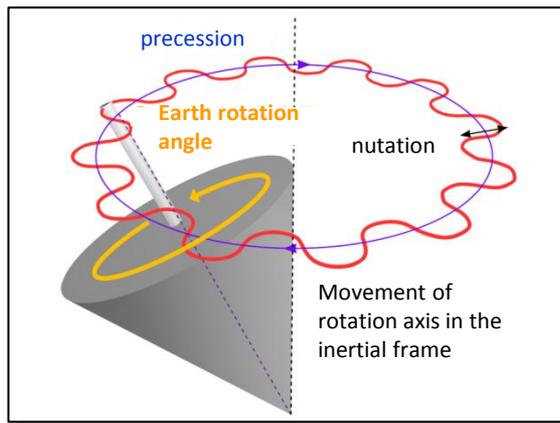
Source: <http://hpiers.obspm.fr/icrs-pc/icrf2/icrf2.html>

## Transformation between the frames by means of Earth rotation parameters

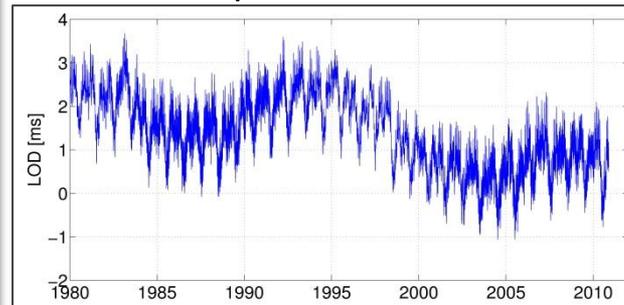
$$\mathbf{x}_{ICRS}(t) = \mathbf{P}(t)\mathbf{N}(t)\mathbf{R}_3(-\theta)\mathbf{R}_2(X)\mathbf{R}_1(Y)\mathbf{x}_{ITRS}(t)$$

- Movement of the Earth rotation axis in the celestial frame (Precession, Nutation)
- Rotation of the Earth about its rotation axis
- Movement of the Earth rotation axis in the terrestrial frame (polar motion)

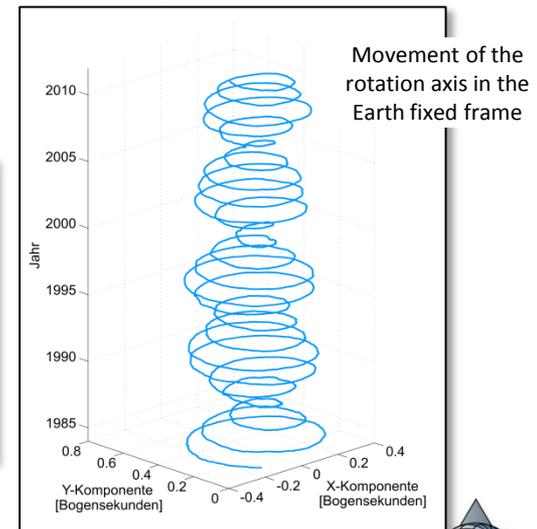
### Precession and Nutation



$$\text{LOD} = -\delta\text{UT1}/\delta t$$

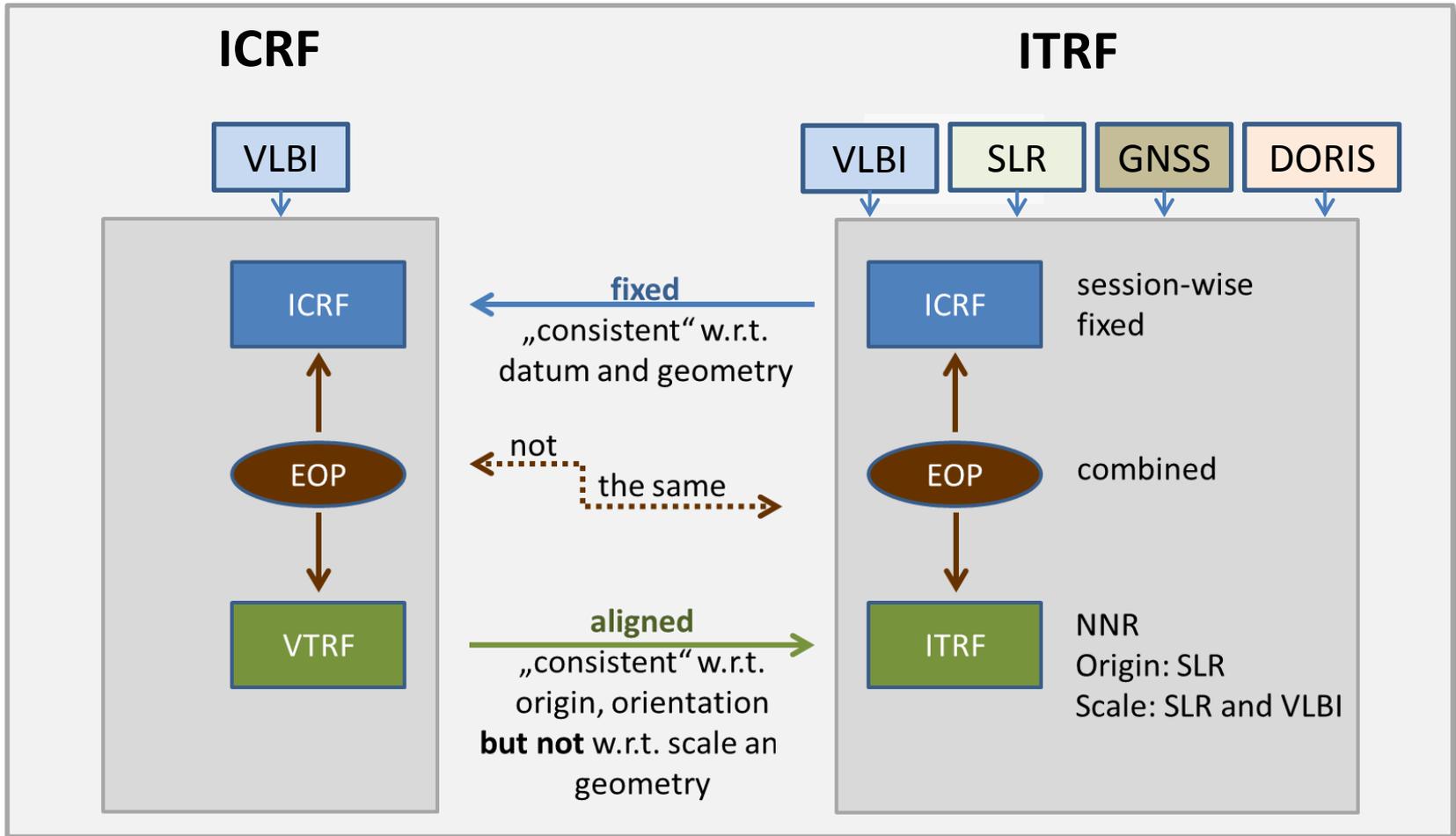


### Polar motion

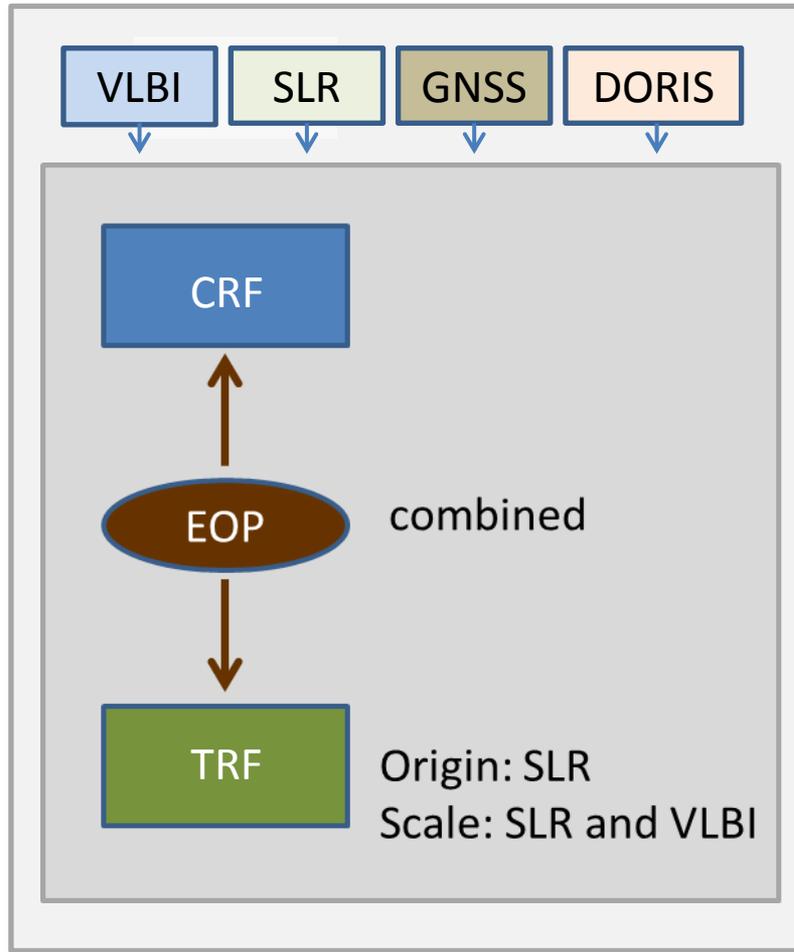


# Computation of ITRF and ICRF

## Current Situation



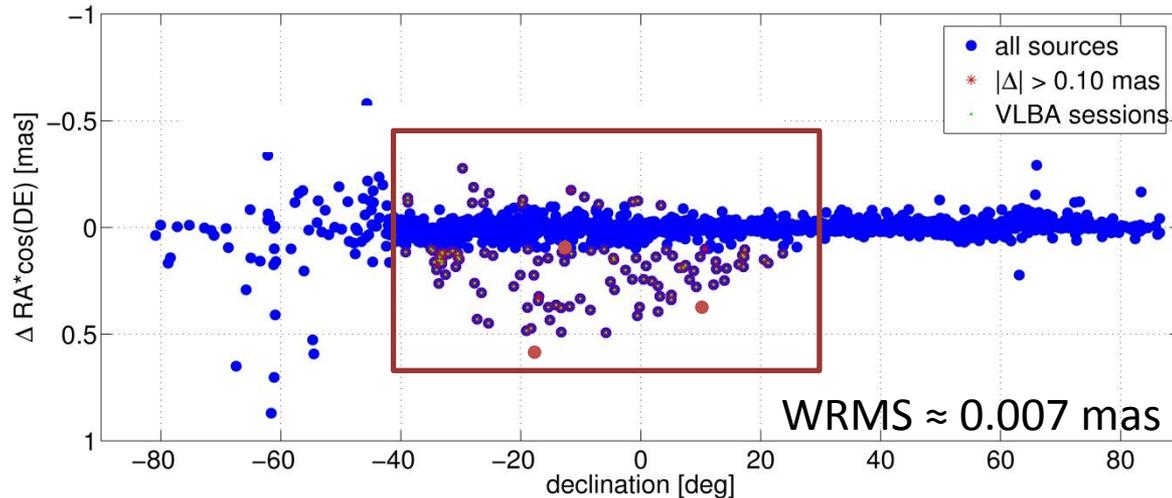
# Consistent computation of TRF and CRF



- TRF, CRF and EOP are estimated simultaneously in one adjustment
  - Origin and scale are realized according to the standards applied for ITRF computation (IERS Conventions)
- $\approx 45\,000$  parameters are estimated

# Consistent computation of TRF and CRF

## Effect in right ascension ( $\alpha$ )



### Marked sources

- $-40^\circ < DE < 30^\circ$
- $|\Delta RA \cdot \cos(DE)| \geq 0.1 \text{ mas}$
- 108 sources in 21 sessions / 18 regional (VLBA) sessions (105 sources)
- EOP of regional VLBI and global GNSS networks show systematic differences
- Effect on CRF due to combination of techniques. Improvement?

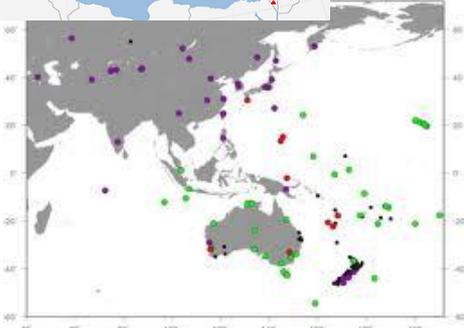
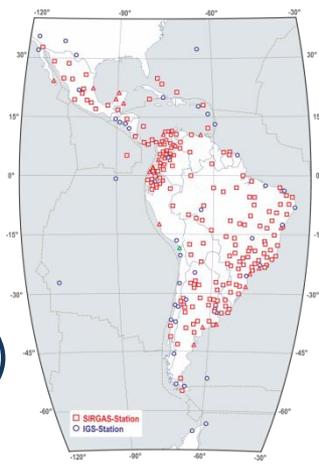
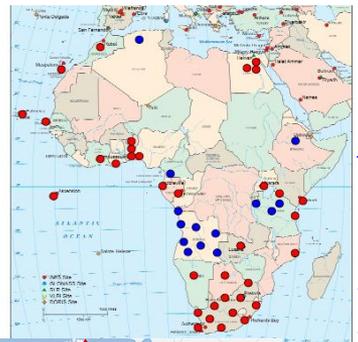
## Regional reference frames

- Their function as densifications of the ITRF
- The example SIRGAS

# Regional reference frames

The ITRF is densified by regional reference frames

- They are the basis for scientific and practical applications with a high temporal and spatial resolution.
- They provide the access to the ITRF on regional and national level.
- They allow for the generation and the use of precise geo-referenced data.
- They are mainly based on GNSS stations (low costs).
- Examples:
  - Africa (AFREF)
  - Asia and Pacific Region (APREF)
  - Europe (EUREF)
  - North America (NAD83)
  - Latin America and Caribbean (SIRGAS)



[http://geodesy.hartrao.ac.za/pastevents/worksop2/Wonnacott\\_AFREF.pdf](http://geodesy.hartrao.ac.za/pastevents/worksop2/Wonnacott_AFREF.pdf)

<http://epncb.oma.be/IAG/results.php>



# Hierarchy of reference frames

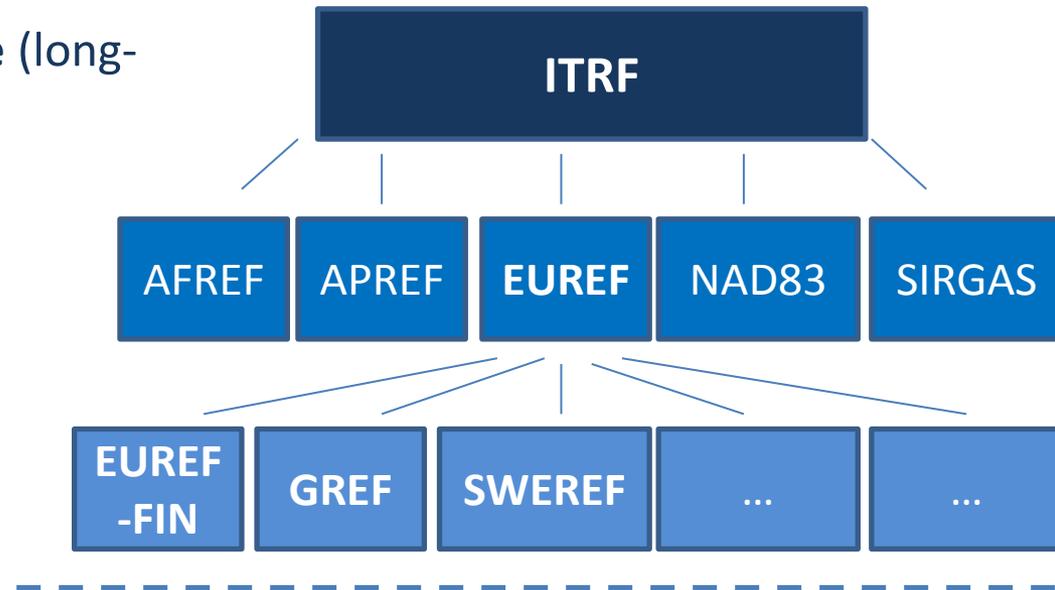
**Global terrestrial reference frame** (long-term solution  $\rightarrow$  [pos, vel, EOP])

**Regional reference frames**

GNSS based (long-term solution)

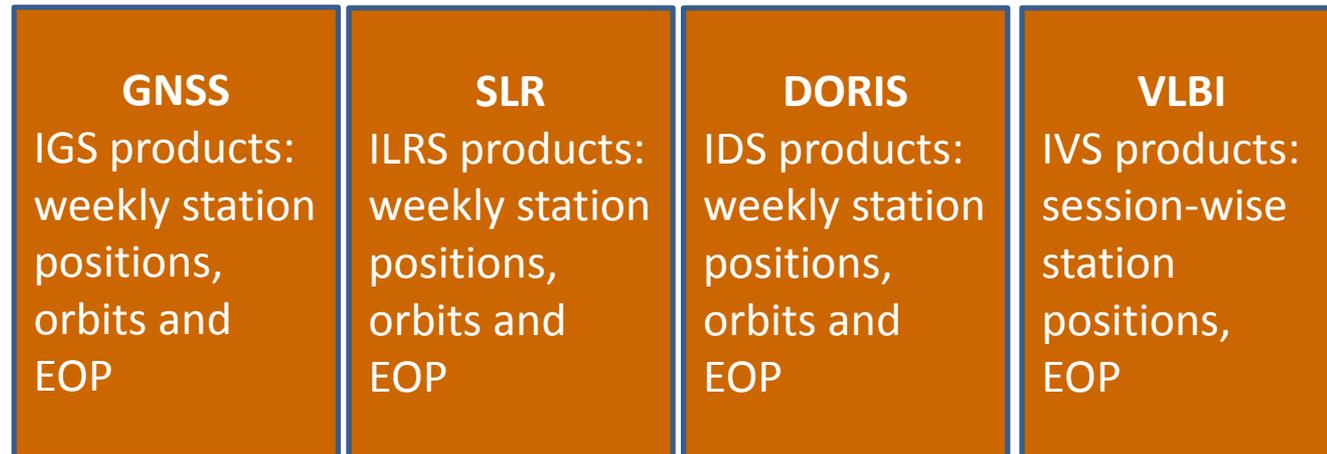
**National reference frames**

GNSS based (long-term solution)



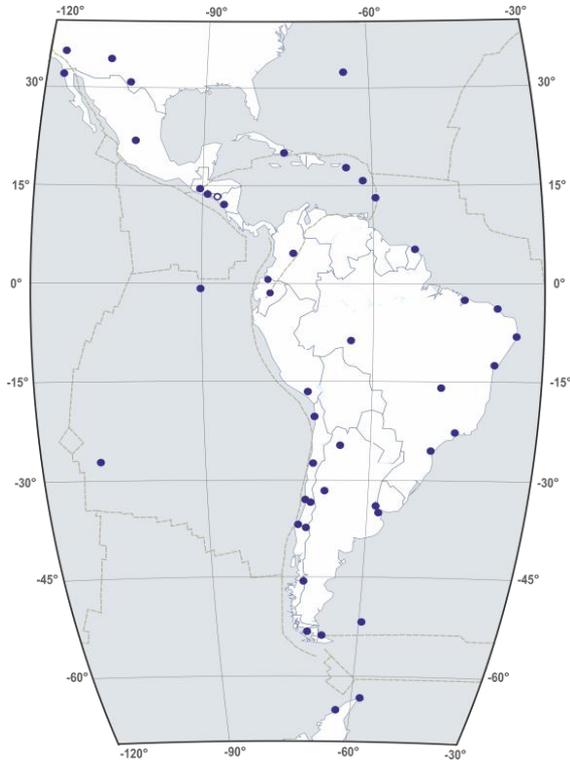
**Short-term global technique specific reference frames**  
(epoch  $\rightarrow$  [pos, EOP])

aligned to ITRF:  
densified by regional epoch frames as well

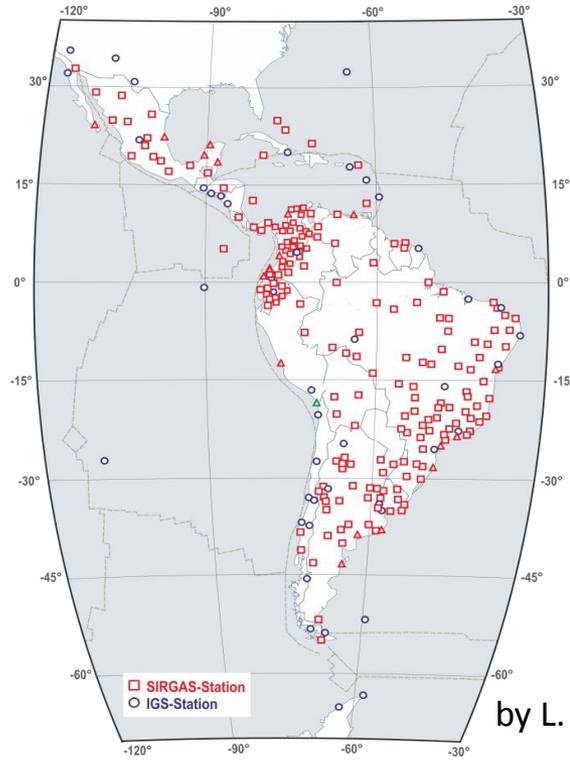


# Example: The regional reference frame SIRGAS

DGFI is responsible for the computation of the reference frame for Latin America and the Caribbean (SIRGAS).



*ITRF stations in Latin America (presently 50)*



by L. Sanchez

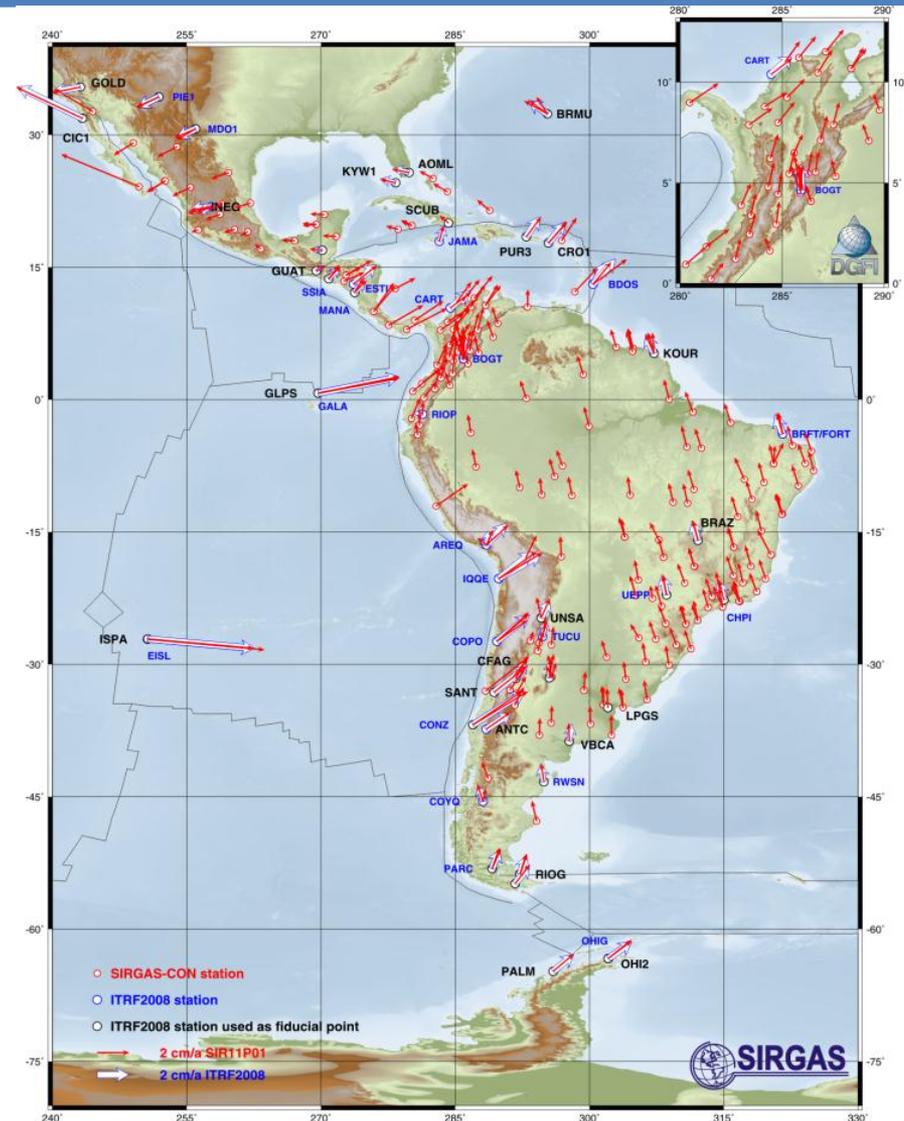
**SIRGAS:** *ITRF densification in Latin America (presently about 300 stations)*

# SIRGAS activities and products

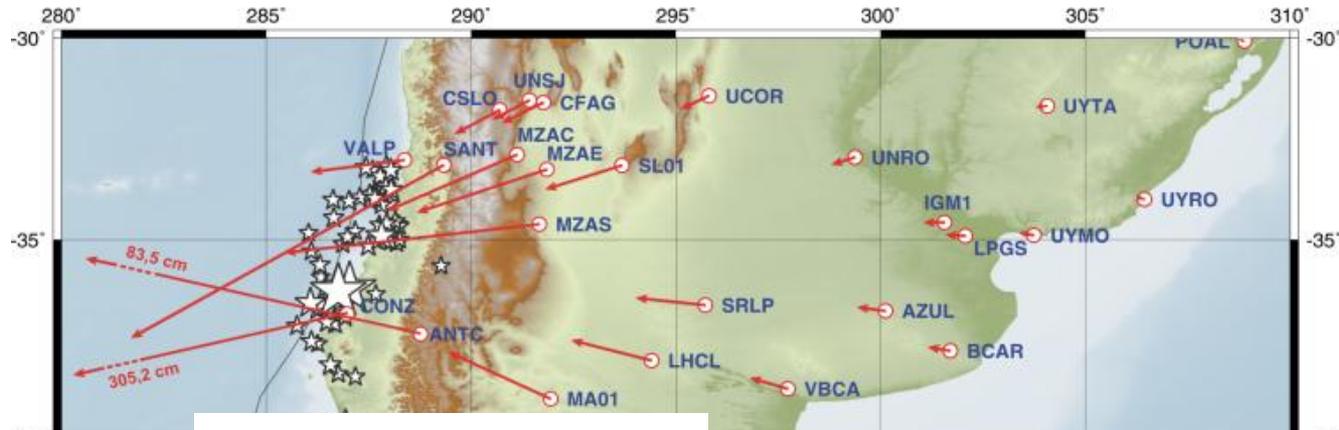
Continuous analysis of the reference frame and publication of

- Weekly station coordinates
- Long-term solutions (constant velocities)
- Time series of station coordinates

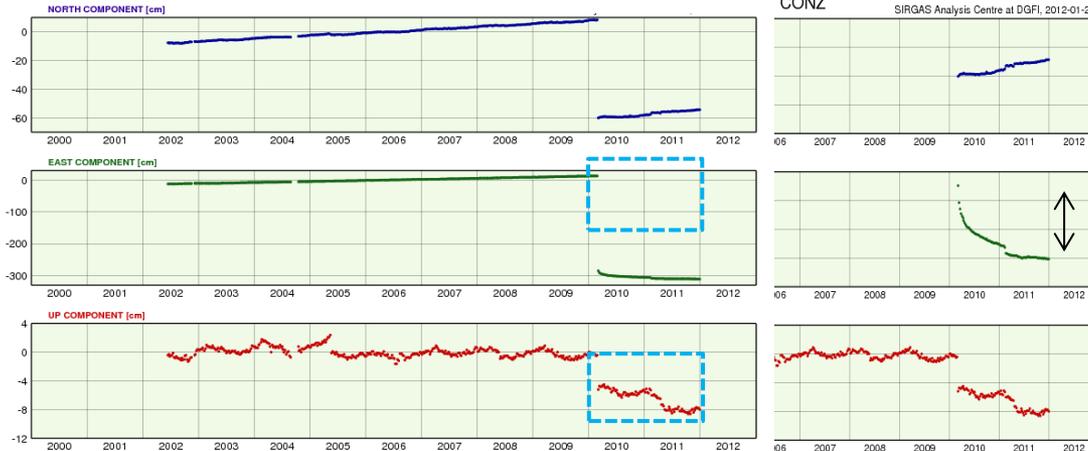
*Horizontal  
velocity field  
of the long-term solution  
SIR11P01*



# Co-seismic movements after the earthquake in Maule, Chile, February 2010



GPS-Station Concepción



10 cm  
 by L. Sanchez  
 Earthquakes with M > 5.0  
 2010 and 06-03-2010  
 20 cm!

ITRF no more valid after the earthquake in that region. Recomputation needs a long time.

→ Fast computation of new coordinates within SIRGAS possible.

# Applications of reference frames

# Applications of reference frames

## Everybody's applications

- Car, ship and plane navigation
- Orientation by using a GPS navigation system and maps with a "GPS grid"
- Land survey by GPS, mapping
- Geocaching

## Examples for geophysical applications

Determination of

- plate tectonics and crustal deformation,
- sea level change,
- post-glacial uplift.

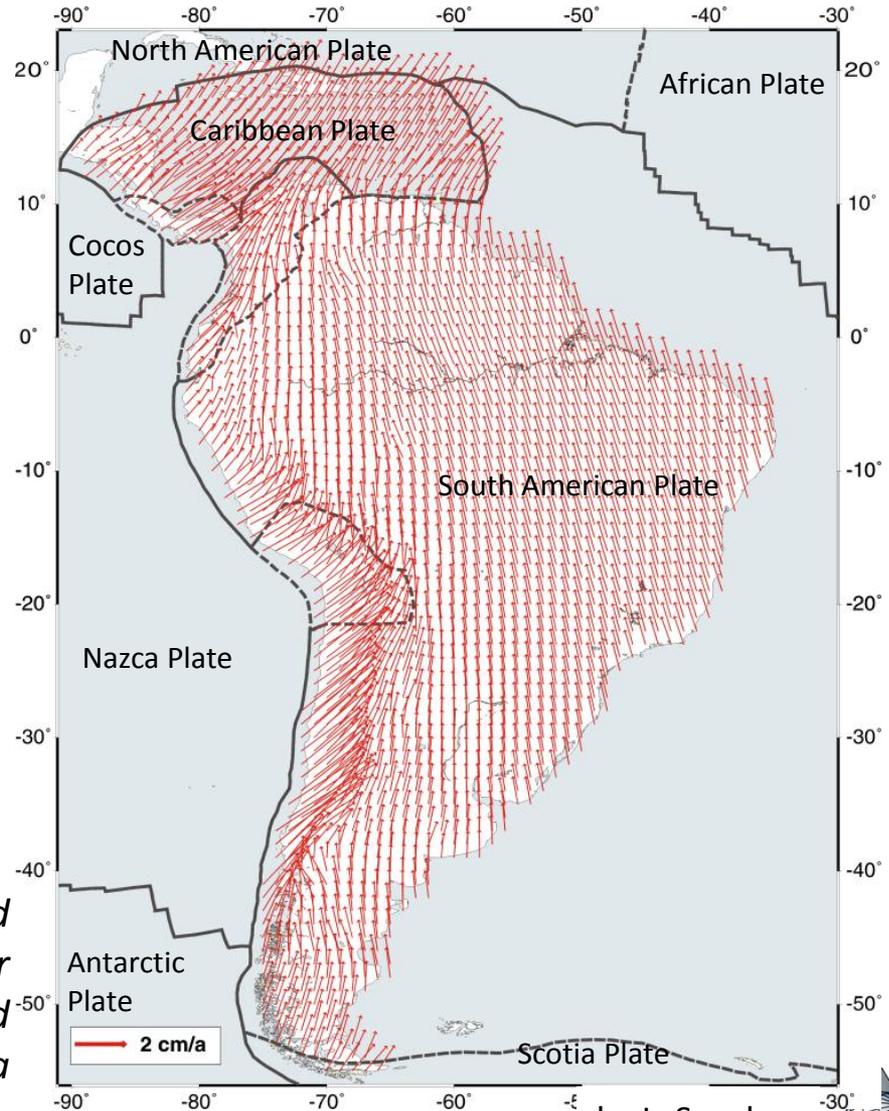
# Application: Plate tectonics and deformation

Modeling of plate motion and deformations of the Earth's surface induced by geophysical processes, e.g.

- Plate tectonics
- Earthquakes

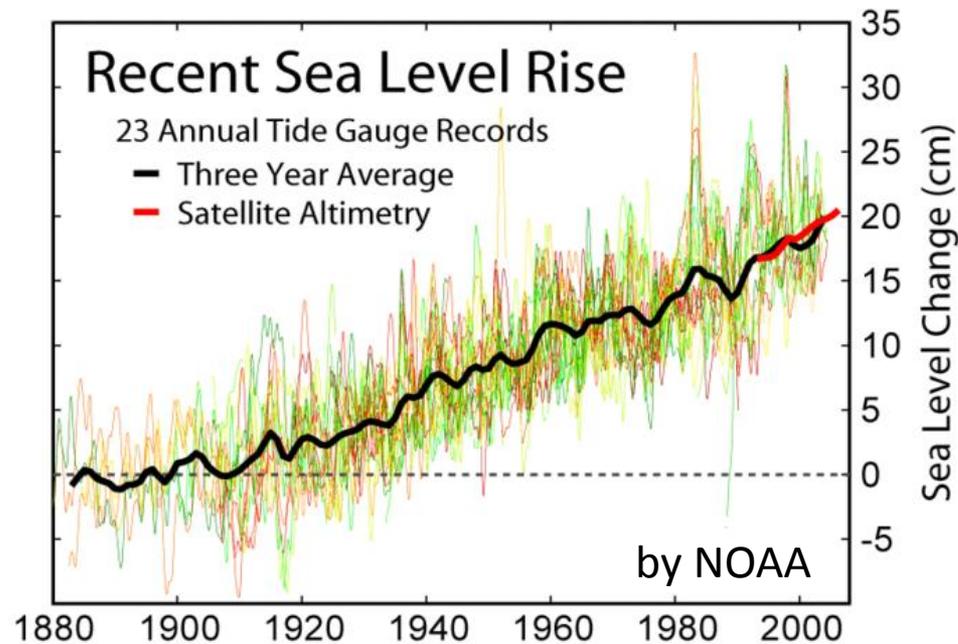
Deformation models allow to study plate tectonics and deformation zones and to predict the station movement in particular for new stations.

*Station movement and deformation model for the Caribbean and Latin America*



by L. Sanchez

## Global sea level rise



### Increasing trend:

Tide gauges: 1.7 mm/yr

Altimetry: 2.6 mm/yr

- Tide gauges are very important for the long-term trend, but they provide only local observations and no observations on the open sea.
- A global and long-term stable reference frame is required to obtain global sea level rise with high accuracy.

# Application: Determination of sea level rise

## Global sea level rise

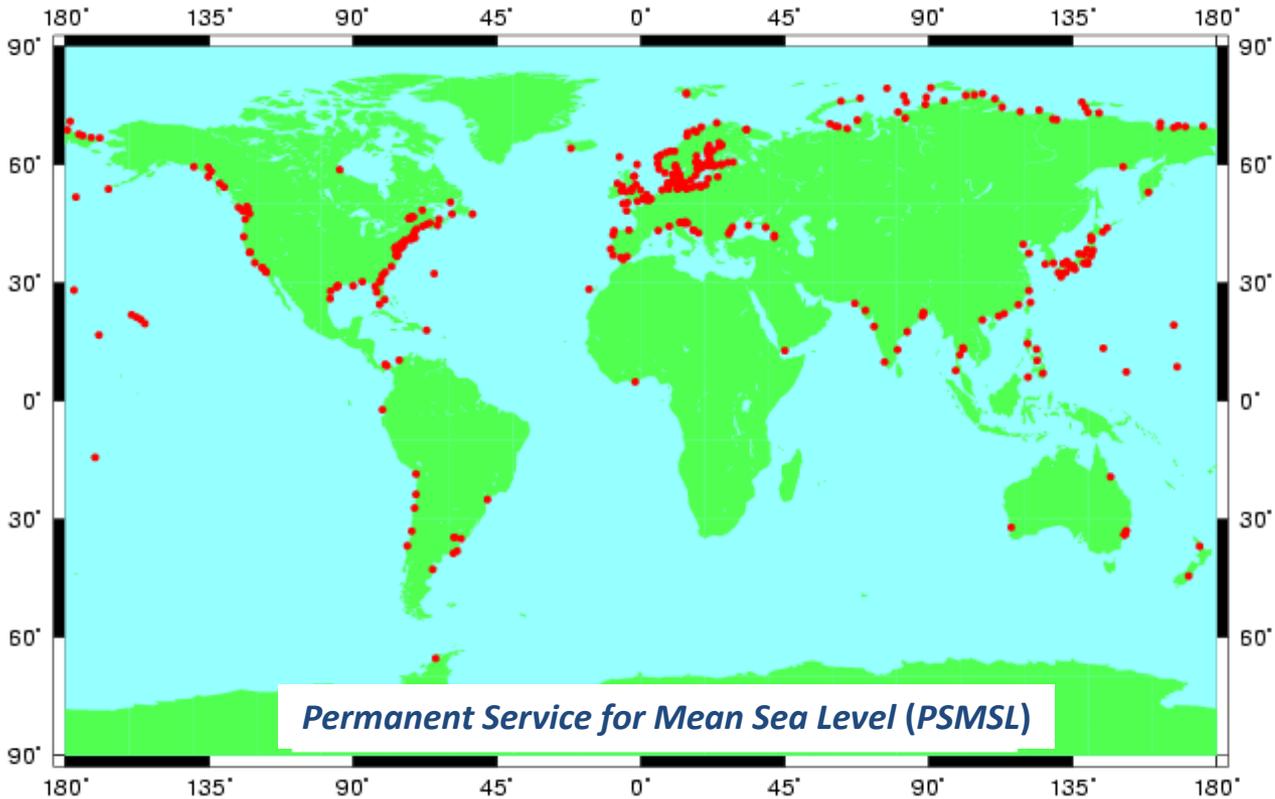


### Today

- Acoustic or radar tide gauges
- Electronic registration with high temporal resolution

# Application: Determination of sea level rise

## Tide gauges at sea coasts (PSMSL data base)

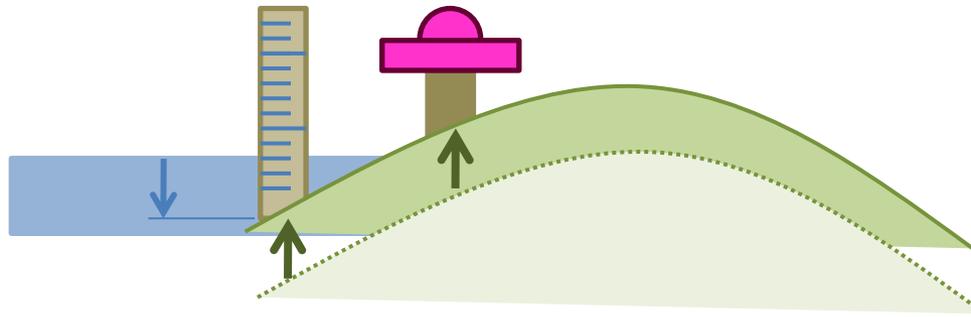


Advantage compared to modern techniques (satellite altimetry): long time series (for some tide gauges more than 100 years).

# Application: Determination of sea level rise

## Tide gauge measurements are relative

- The tide gauge observes the sea level relative to its position.
- But what to do, when the site is moving?



- The site motion has to be determined with respect to a global reference frame. → GPS stations are installed in immediate proximity of the tide gauges.

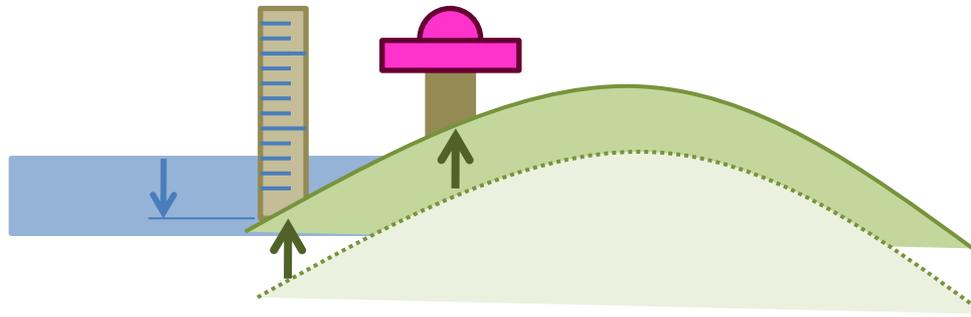
$$\text{sea level rise} = \text{tide gauge} + \text{GPS measurement}$$

- One reason for an uplift of tide gauge stations is the postglacial rebound. Not correcting for the effect would lead to a falsification of sea level rise for a large region and thus to a wrong global sea level rise.

# Application: Determination of sea level rise

## Tide gauge measurements are relative

- The tide gauge observes the sea level relative to its position.
- But what to do, when the site is moving?



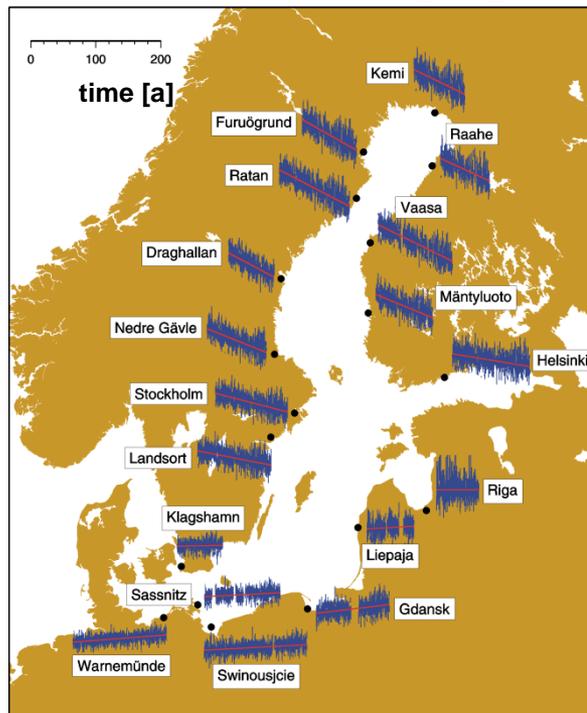
- The site motion has to be determined with respect to a global reference frame. → GPS stations are installed in immediate proximity of the tide gauges.

sea level rise = tide gauge + GPS measurement

→ without a global reference frame (represented by the GPS stations and the GPS orbits), the global sea level rise can not be determined

## The apparent lowering of sea level in Scandinavia

Time series of tide gauges



Ice coverage in Scandinavia during the last ice age



Postglacial uplift of 1 cm/year due to the melting of the ice sheet after the last ice age. → A very slow and thus long-lasting process.

## The Helsinki tide gauge

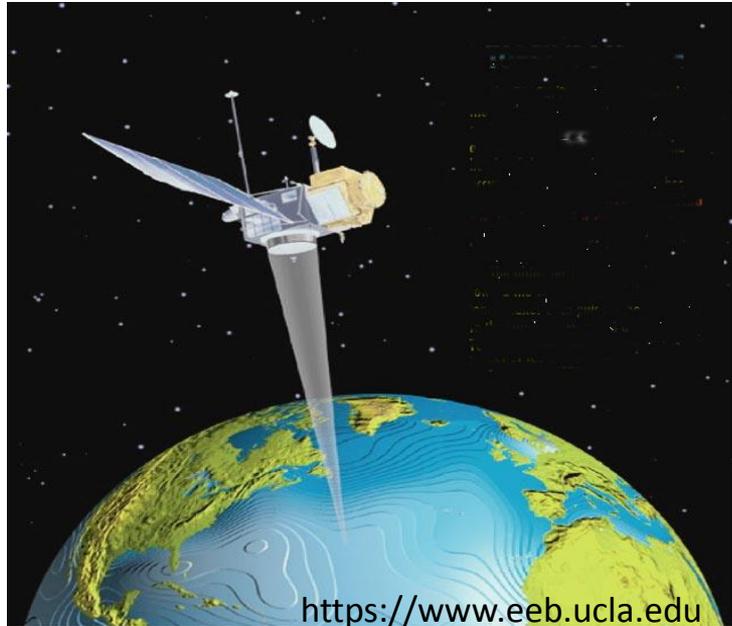


The Helsinki tide gauge is inside this hut.  
A GPS station on a granite pillar is close by.

The GPS station is not only used for  
referencing the tide gauge but also by the  
Geocache community for calibrating their  
(quote) toys.  
( <http://www.geocaching.com> )

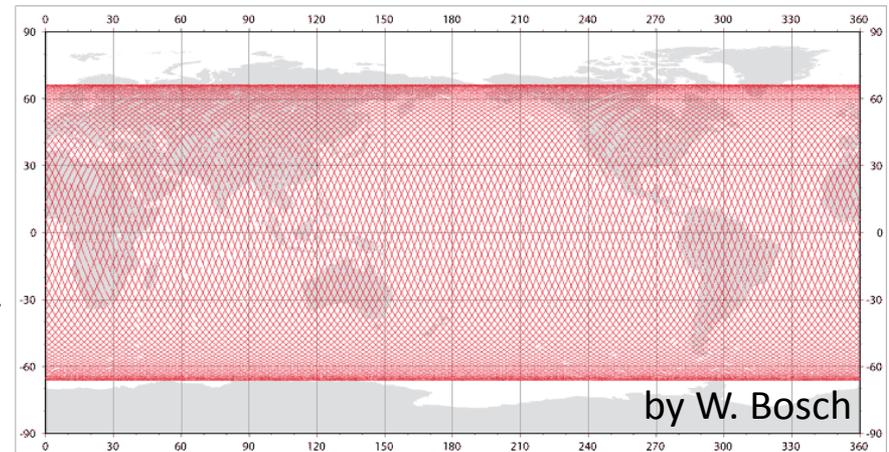
# Application: Determination of sea level rise ...

## ... from Altimetry missions



Altimetry measures the time taken by a radar pulse to go from satellite to the sea surface and back to the satellite receiver.

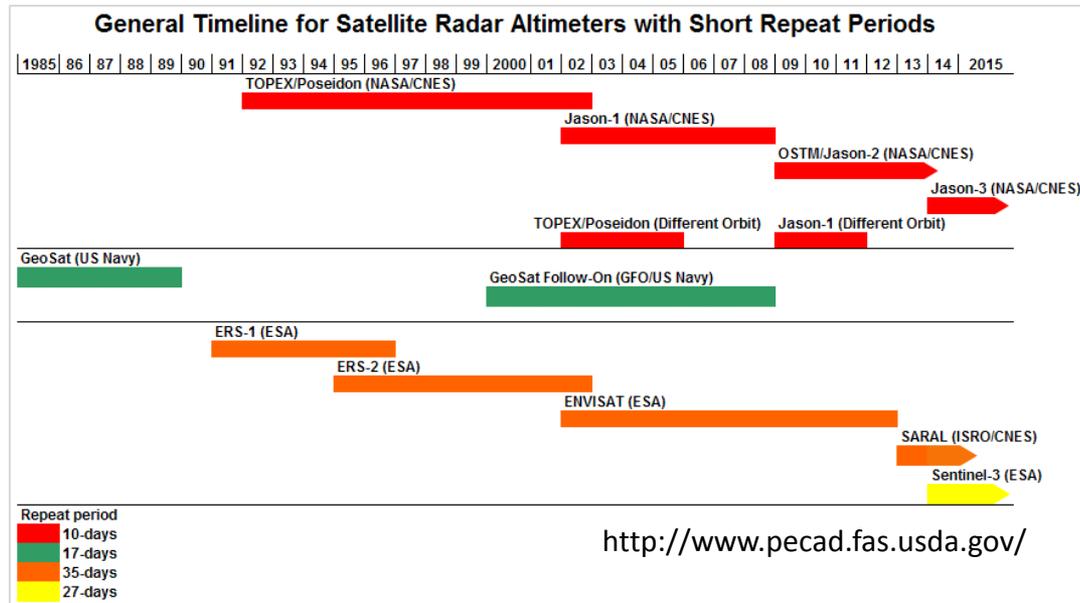
Altimetry provides a global data set.



*Ground tracks of  
TOPEX/Poseidon  
mission*

# Application: Determination of sea level rise ...

## ... from Altimetry missions



- At least two missions in parallel since 1992.
- Global coverage and high spatial density of observations.

# Application: Determination of sea level rise

## Sea level change and ITRF

TRF errors readily manifest as spurious sea level rise accelerations

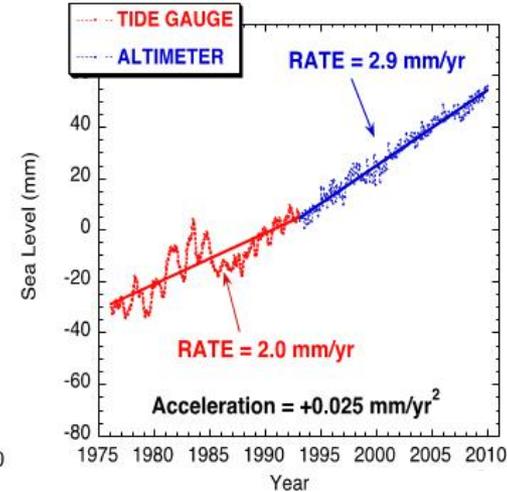
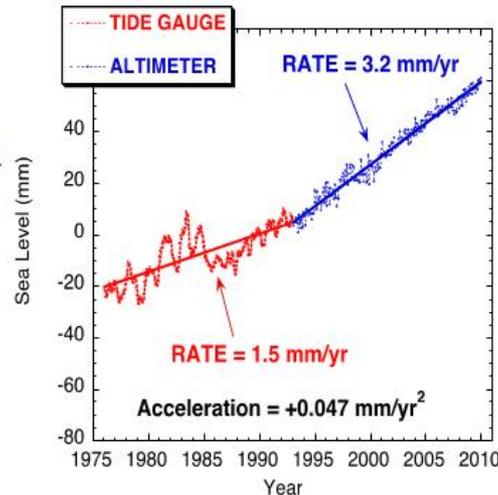
**Left: ITRF2005**

(based on Church and White, 2011)

**Right: ITRF2000**

(simulated into the Church and White records)

YEB, September 2012



by Y. Bar-Server, JPL

→ All satellite orbits must be determined in the same reference frame with high accuracy in order to obtain the global sea level change. Reference frame errors can affect the sea level change significantly.

# Application: Determination of sea level variation

## Research: GNSS-tide gauges

Sea level measurement based on GNSS only using reflected GNSS-signals:

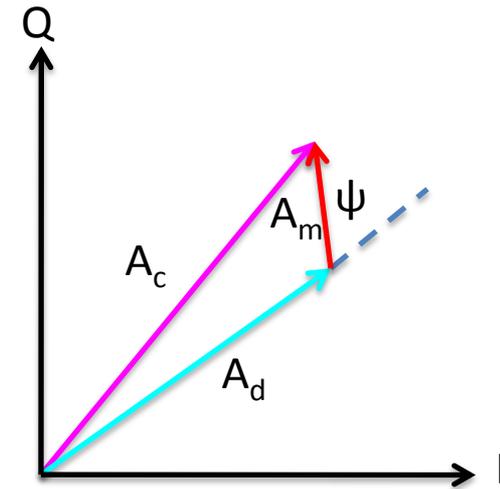
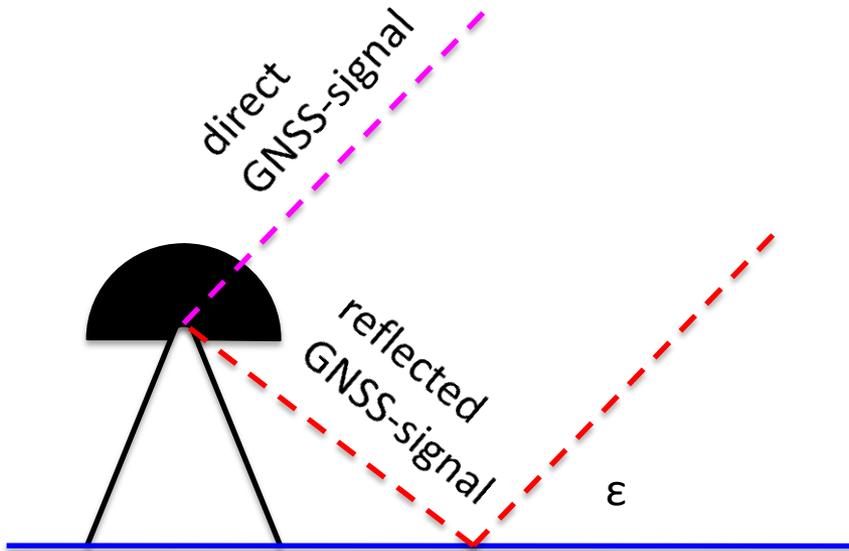
- a) SNR-analysis with standard coastal GNSS-installations (e.g. Brest FR)
- b) Geodetic GNSS analysis with two-antenna installations (e.g. Onsala, SE)



Onsala Space Observatory (OSO), Sweden

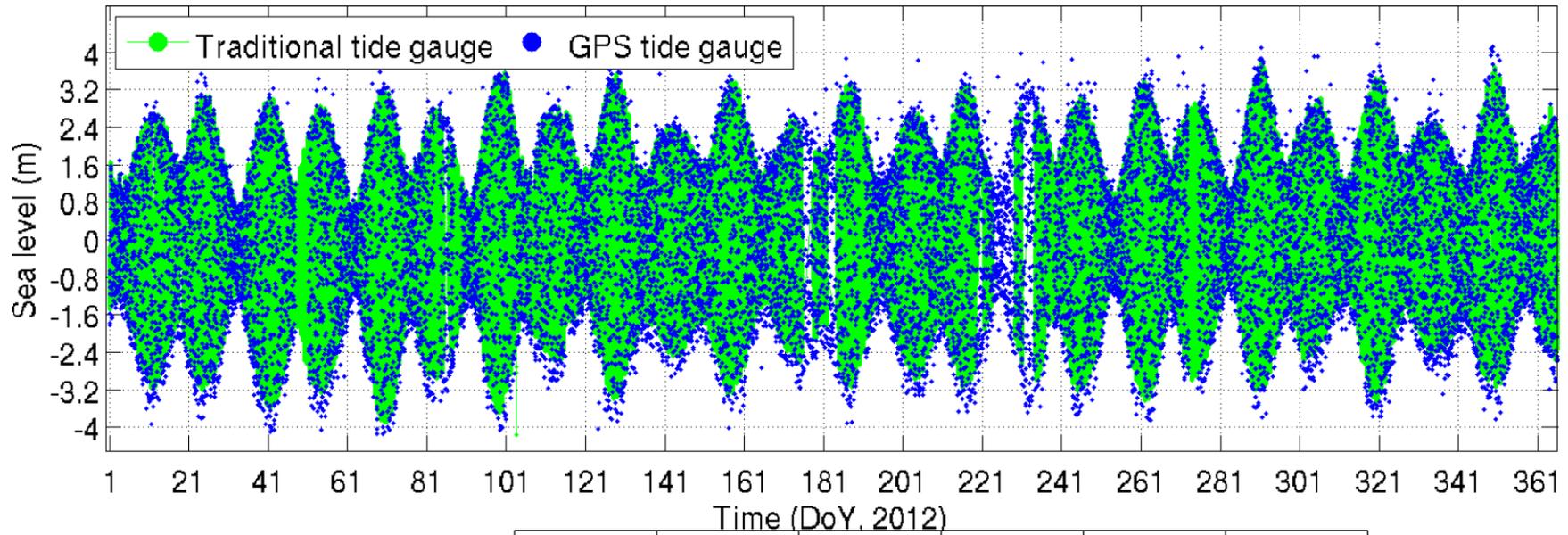


# GNSS-tide gauge with SNR-analysis, e.g. Brest

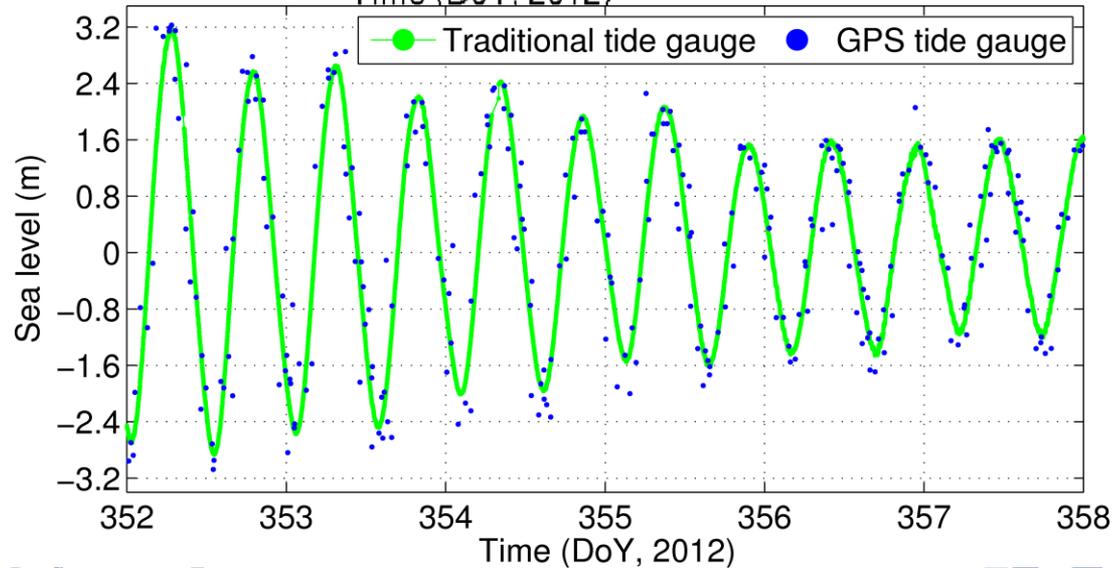


- GNSS receiver:  $SNR^2 = A_c^2 = A_d^2 + A_m^2 + 2 A_d A_m \cos \psi$
- Multipath varies with:  $d\psi/dt = (2\pi/\lambda) 2 h \cos \varepsilon (d\varepsilon/dt)$
- SNR varies with:  $SNR = A_c \cos (4\pi h/\lambda \sin \varepsilon + \phi)$
- Literatur: t.ex. Georgiadou & Kleusberg (1988); Bilich *et al.* (2007); Larson *et al.* (2007); Löfgren *et al.* (2011); Larson *et al.* (2013)

# GNSS-tide gauge with SNR-analysis, e.g. Brest

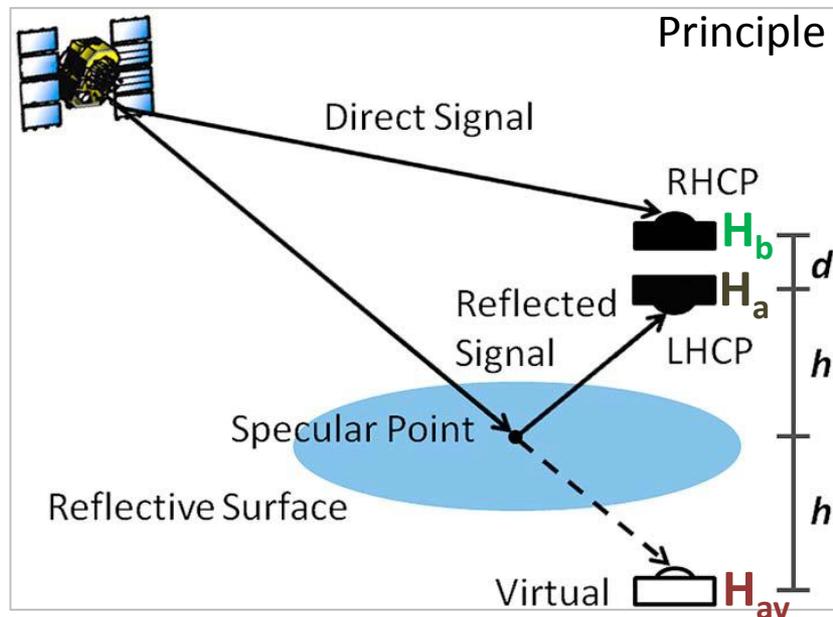


IGS station  
Brest, France



## Research: GNSS-tide gauge with two-antennas

Sea level measurement based on GNSS only.



Löfgren et al. 2011

Instrument consists of two GNSS antennas. The height difference  $d$  of the antenna reference points is known with high accuracy.

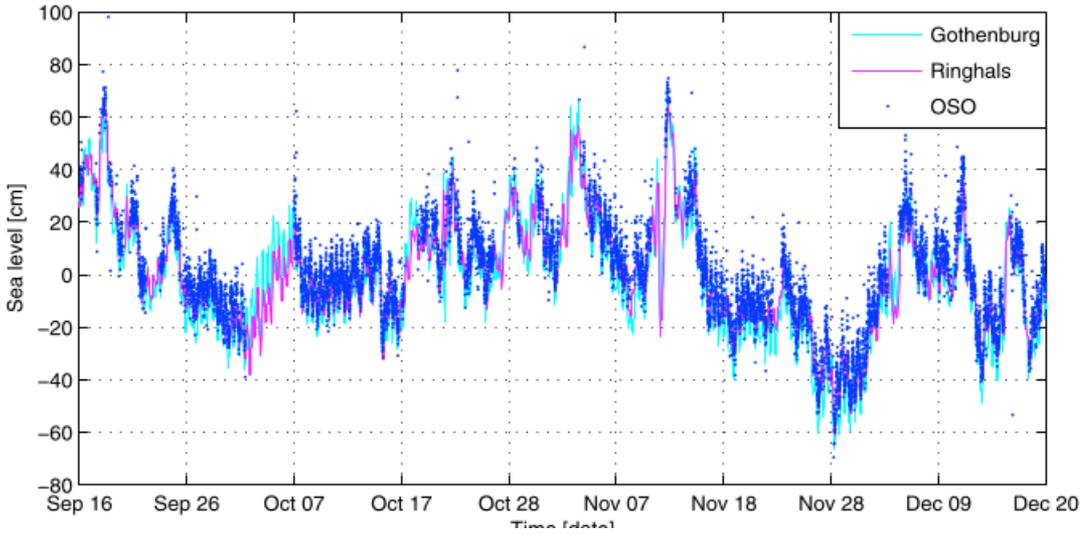
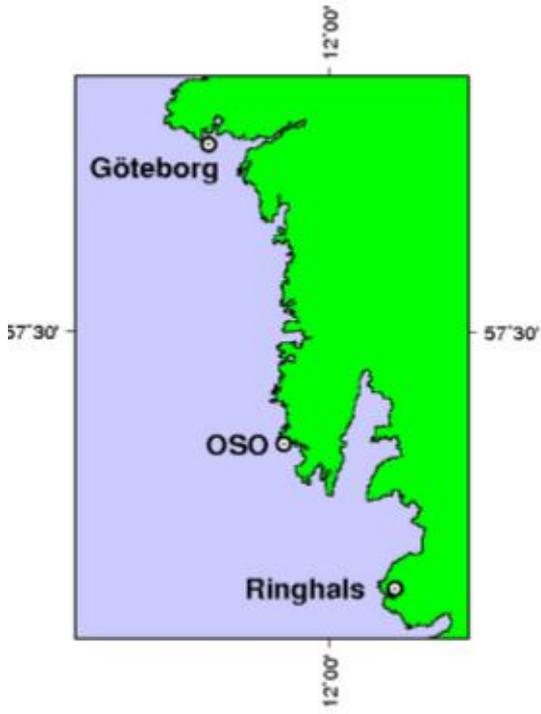
- **b**: Upper antenna, right hand polarized: direct GNSS signals.
- **a**: Lower antenna, upside down, left hand polarized: GNSS signals reflected by the sea surface.  
→ virtual height of **a**

$$H_{av} = \text{sea level height} - h$$

$$\text{Sea level height} = \frac{(H_b - d + H_{av})}{2}$$

# GNSS-tide gauge with geodetic GNSS analysis: OSO

## Comparison of OSO and two stilling well tide gauges



Löfgren et al. 2011

# Summary

- The ITRF is computed from the combination of different space geodetic techniques by exploiting their individual strengths.
- VLBI is essential for ITRF because
  - it gives the link to the ICRF
  - of its high accuracy and long-term stability
- The consistency of ITRF and ICRF and the related EOP as well as the consideration of non-linear station motions are important research topics in the next years.
- Regional reference frames allow to access to the ITRF on regional level. The high (GNSS) station density ensures a high frame accuracy.
- Many geophysical applications require a high accuracy of the reference frame (e.g. the determination of the sea level change).
- The accuracy requirement specified for GGOS is 1mm and 0.1mm/yr for positions and velocities, respectively. This target is not yet reached and more research in the field of reference frame computation is necessary.

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